



Regional Technical Seminar

Short Circuit Design Considerations

Transformer Regional Technical Seminar
Tampa , FL
February 11, 2025

waukesha
a prolec ge company

William Snowden Electrical Design Engineer

William Snowden joined Prolec GE Waukesha in November 2022 after graduating from North Carolina State University with a Bachelor of Science Degree in Electrical Engineering. At the Goldsboro facility, he manages the quote design process and has designed and quoted medium power transformers up to 230 kV and 60 MVA.



Agenda

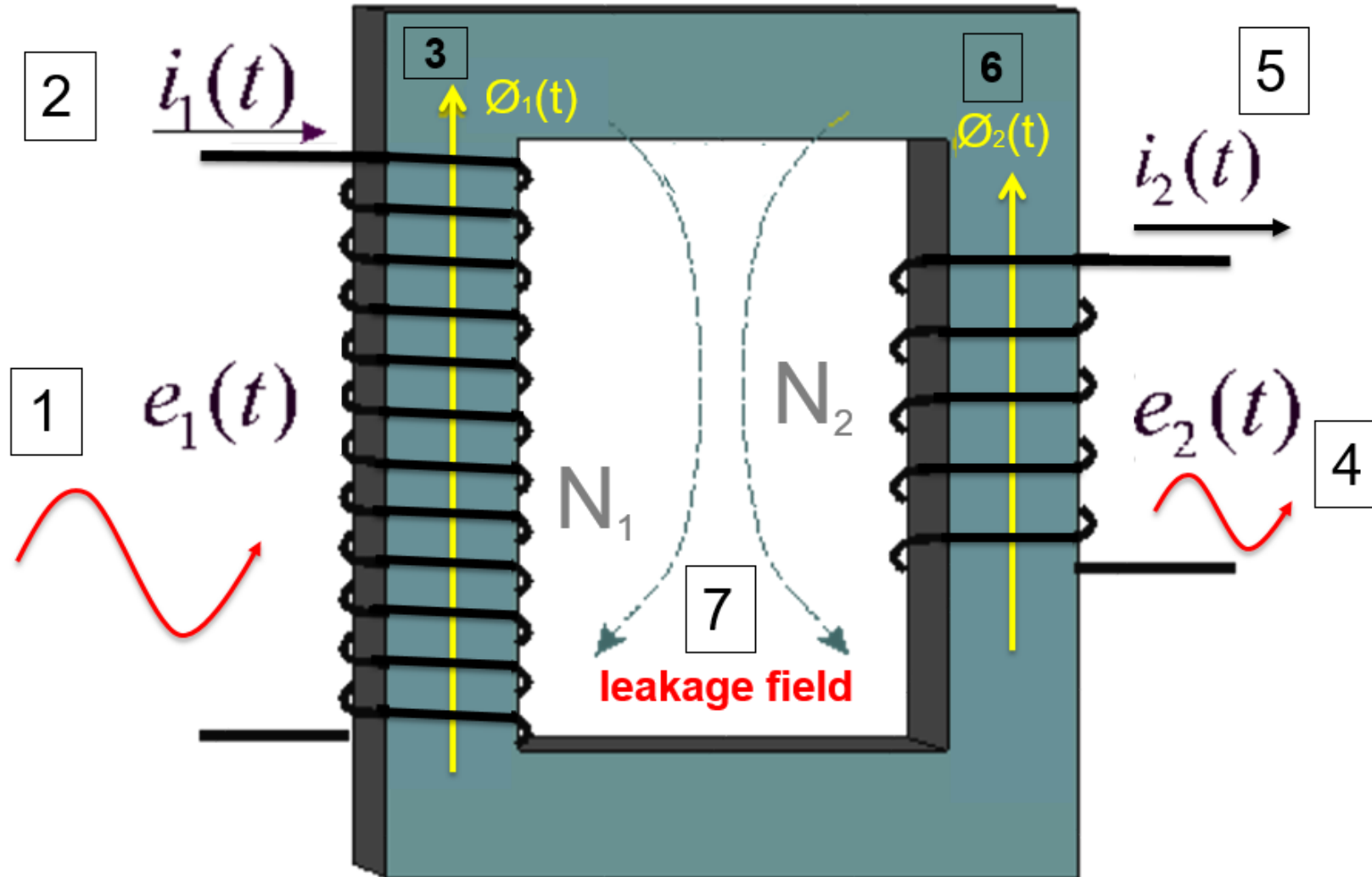
- Review transformers: How they work (textbook vs reality)
- Visualize relationship between Current and Magnetic Forces
- Understand fault current from time $t = 0$ to $t = ?$
- Understand formulas and variables to calculate short circuit currents
- Discuss fault types
- Calculation Example: Calculate short circuit amps
- Get a mental picture of magnetic forces acting within a transformer resulting from short circuit



Part 1 – Transformer Basics:

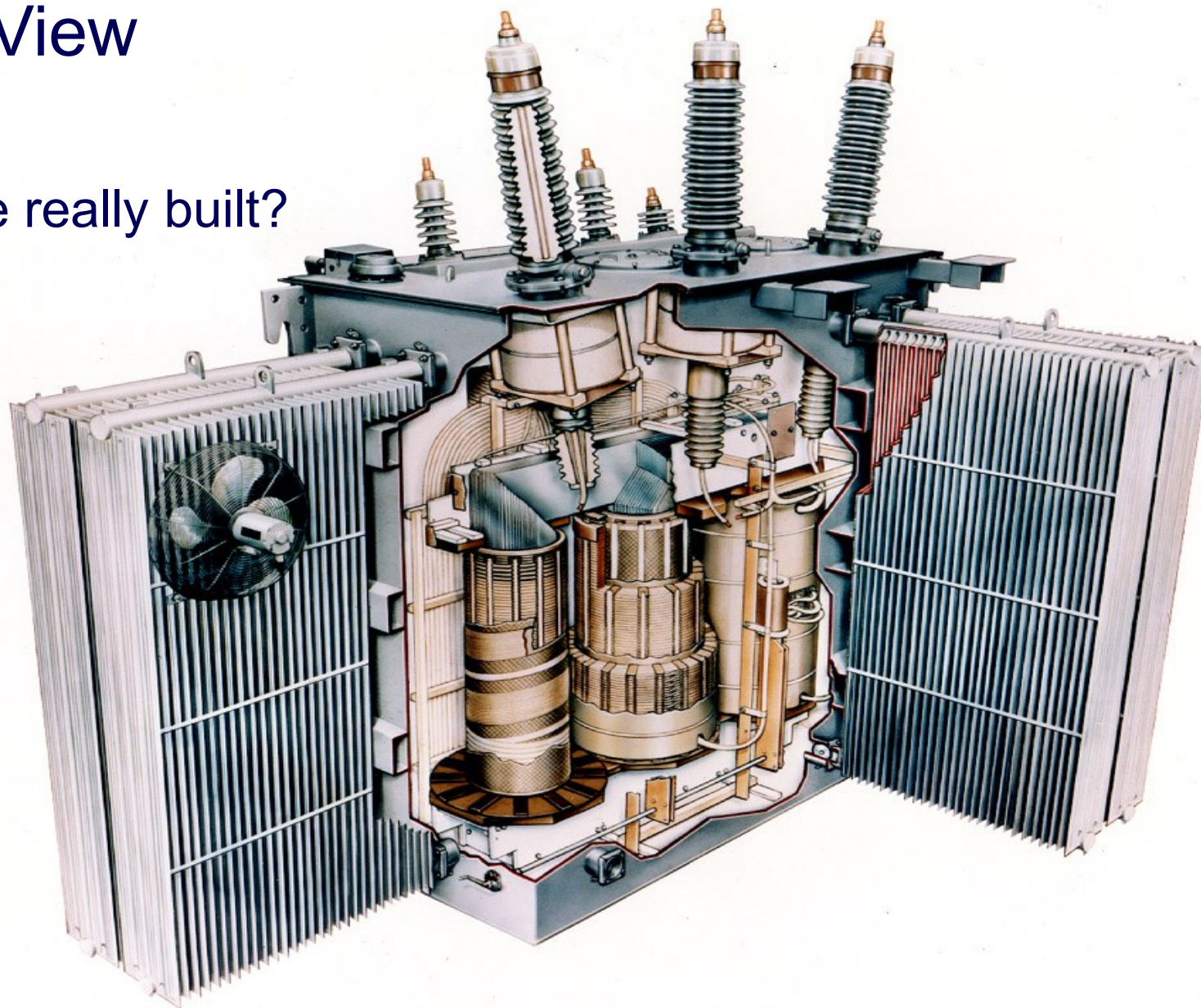
- How they work
- How they are actually built

Textbook Transformer (step by step)

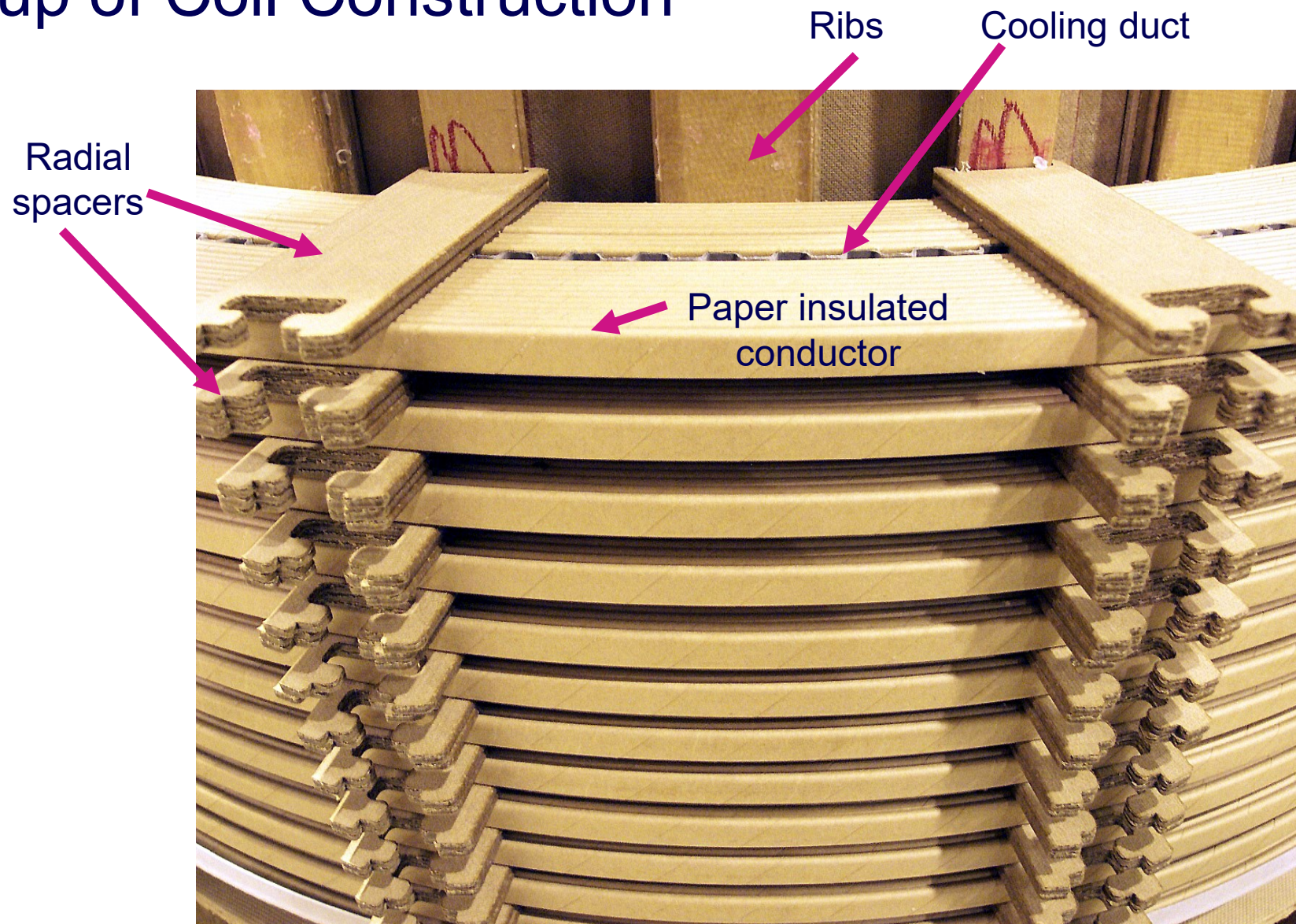


Cutaway View

How they are really built?



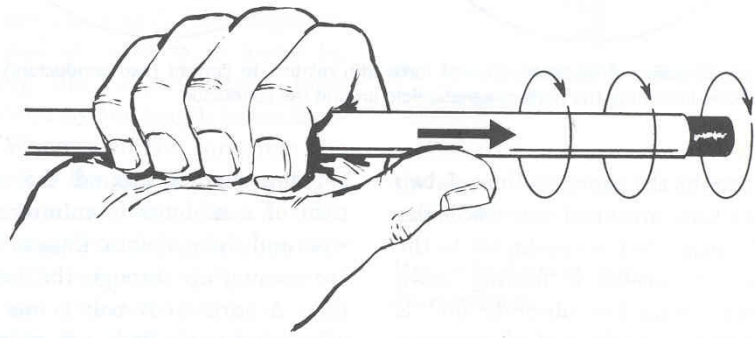
Close up of Coil Construction



Part 2 – Transformer Basics:

- Fundamentals of Magnetics and Forces
- Magnetic Fields Around Conductors
- Forces That Result

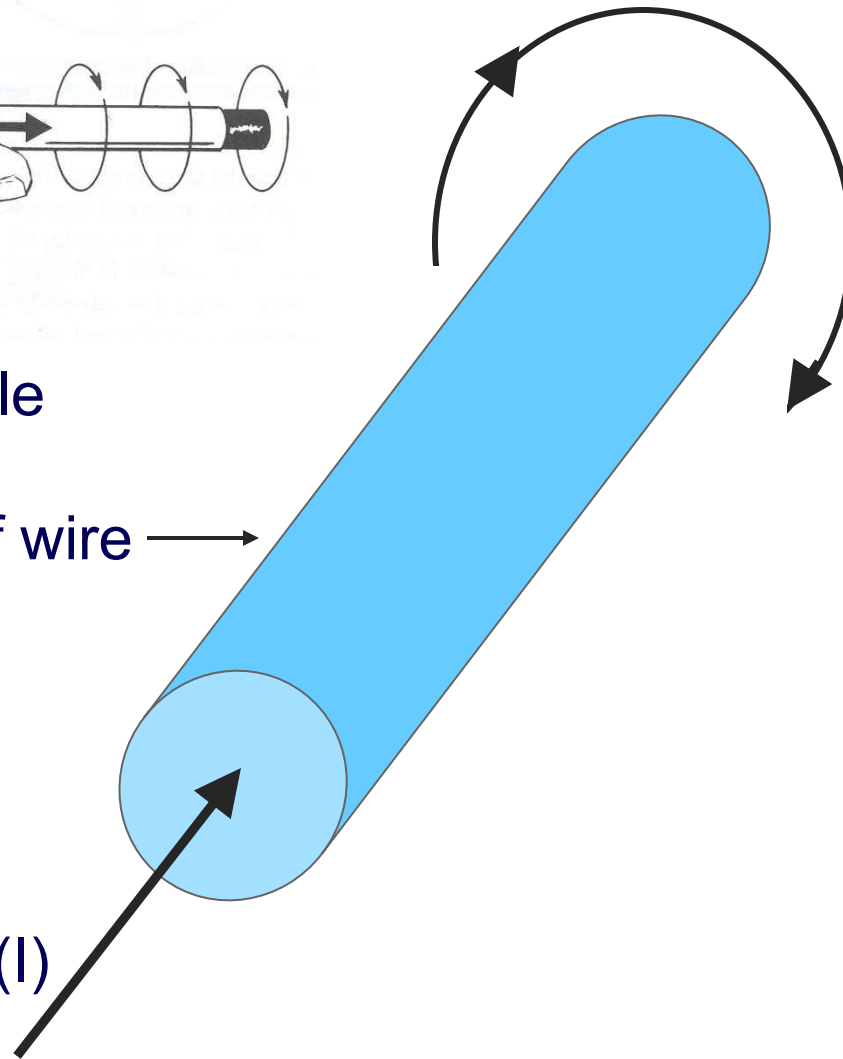
Current & Magnetic Field Relationships



Right hand rule

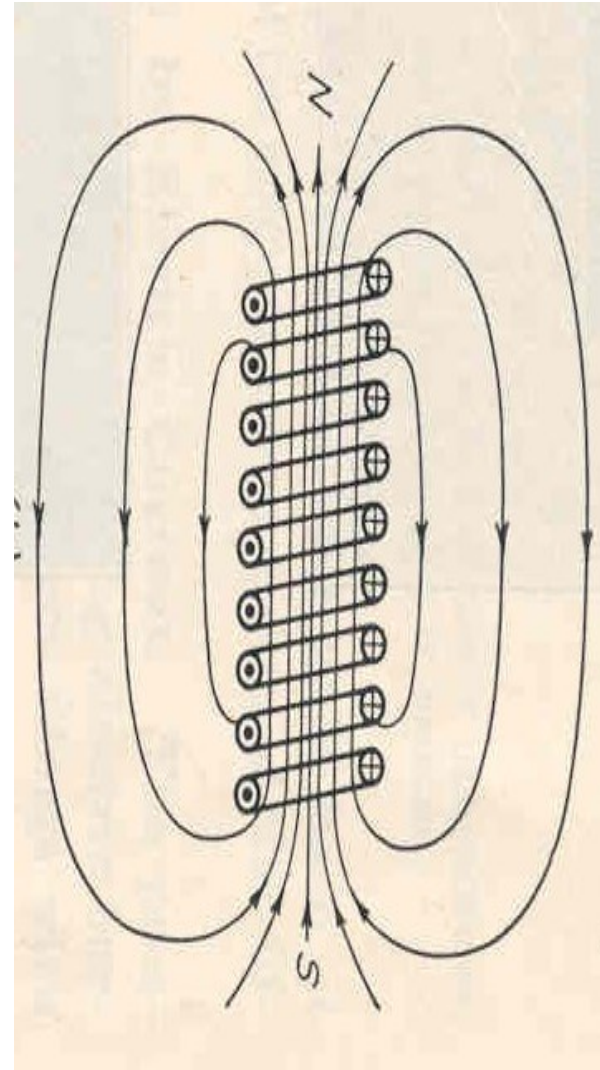
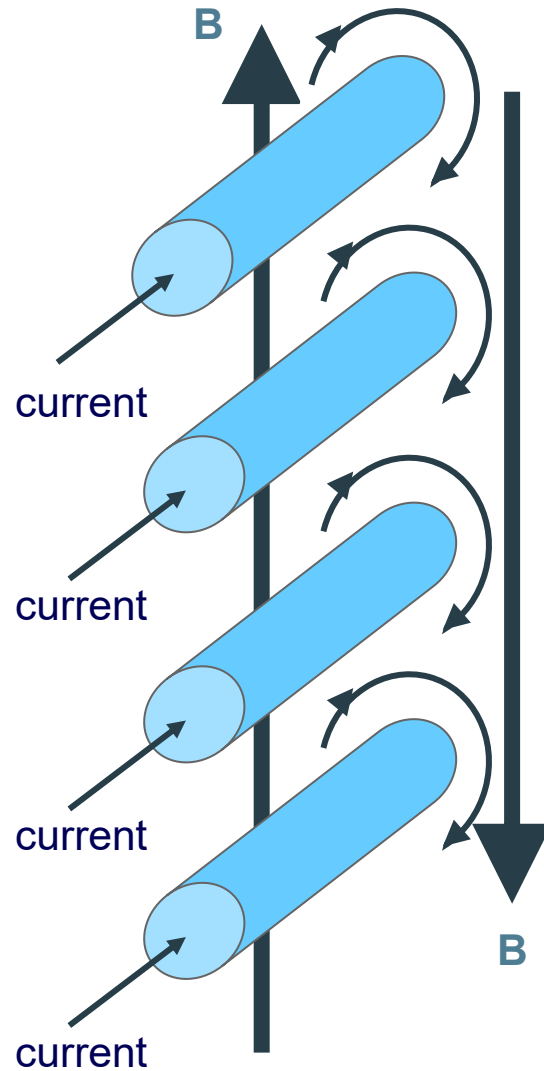
Consider a section of wire →

Current Flow (I)



resulting
magnetic
field direction
(CW)

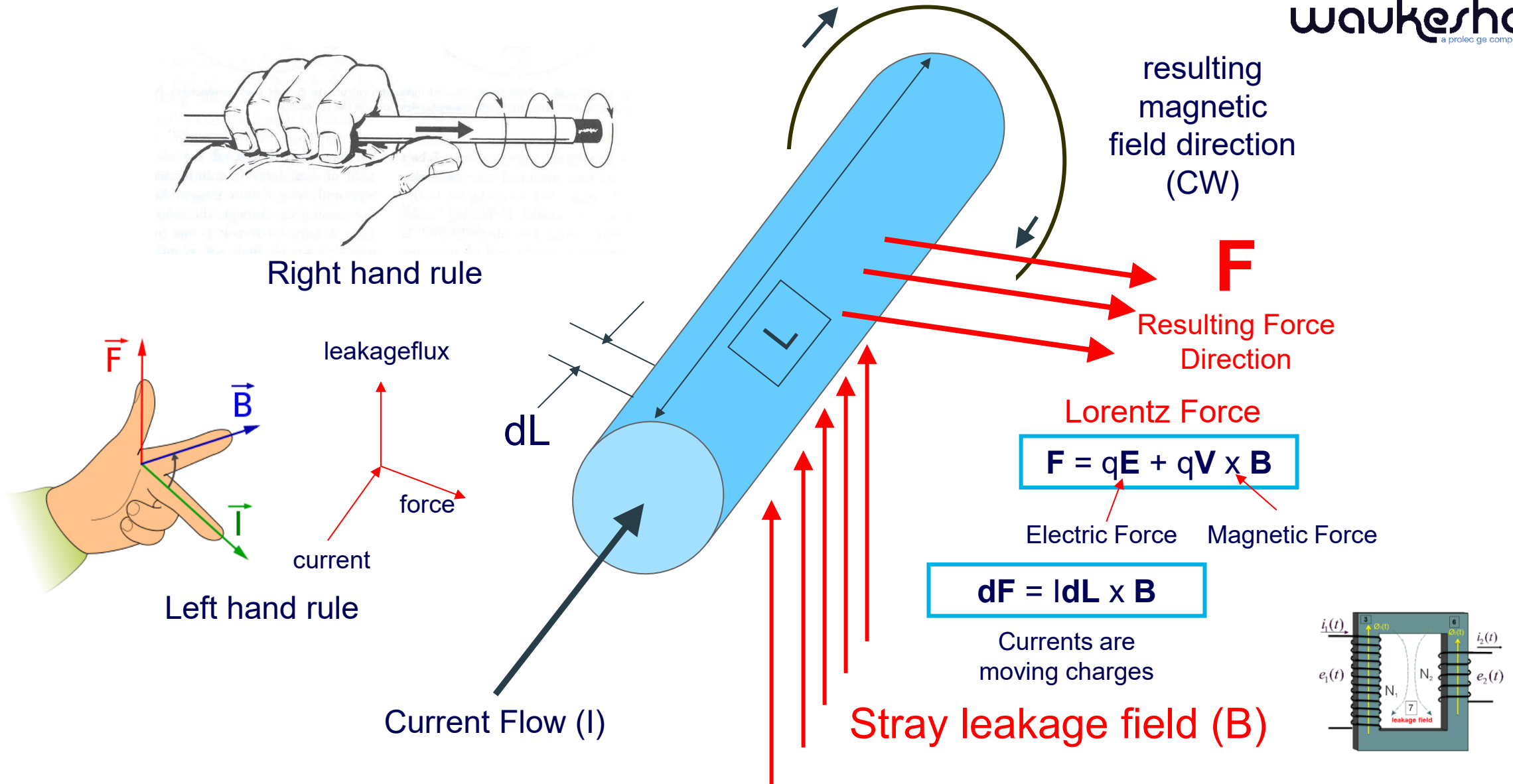
Effect of Many Turns



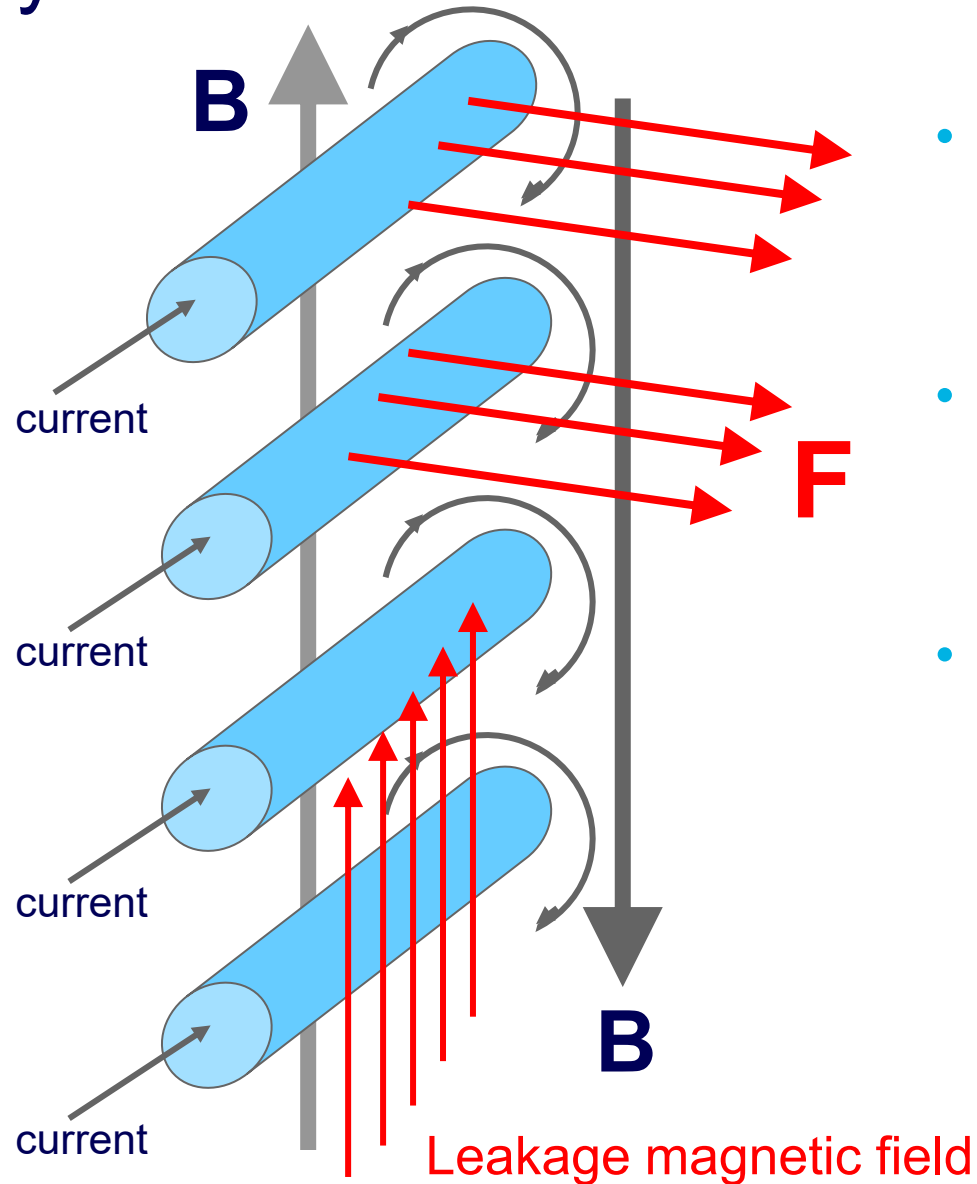
- Fields at inner/outer edges add together.
- One uniform magnetic path results
- Magnetic field (B) intensifies with # turns (N) or the current (I).

$$B \propto NI$$

Leakage Field / Current / Force Relationships



Effect of Many Turns



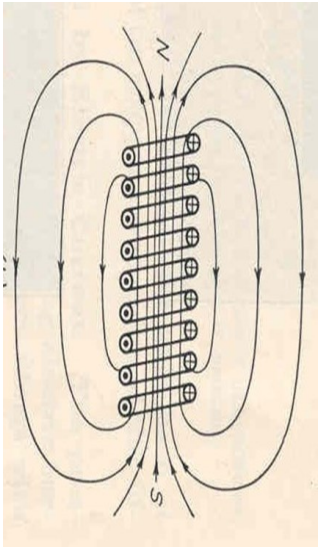
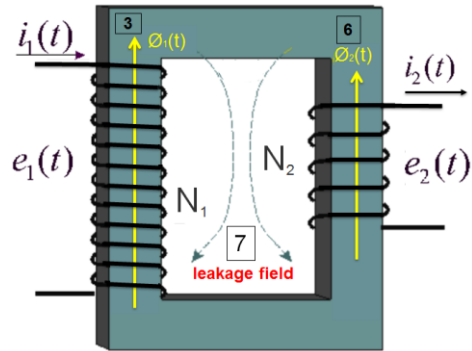
- Fields at inner/outer edges add together
- One uniform magnetic path results
- Magnetic Forces (F) intensifies with # turns (N)

$$B \propto NI$$

$$F = NIL \times B$$

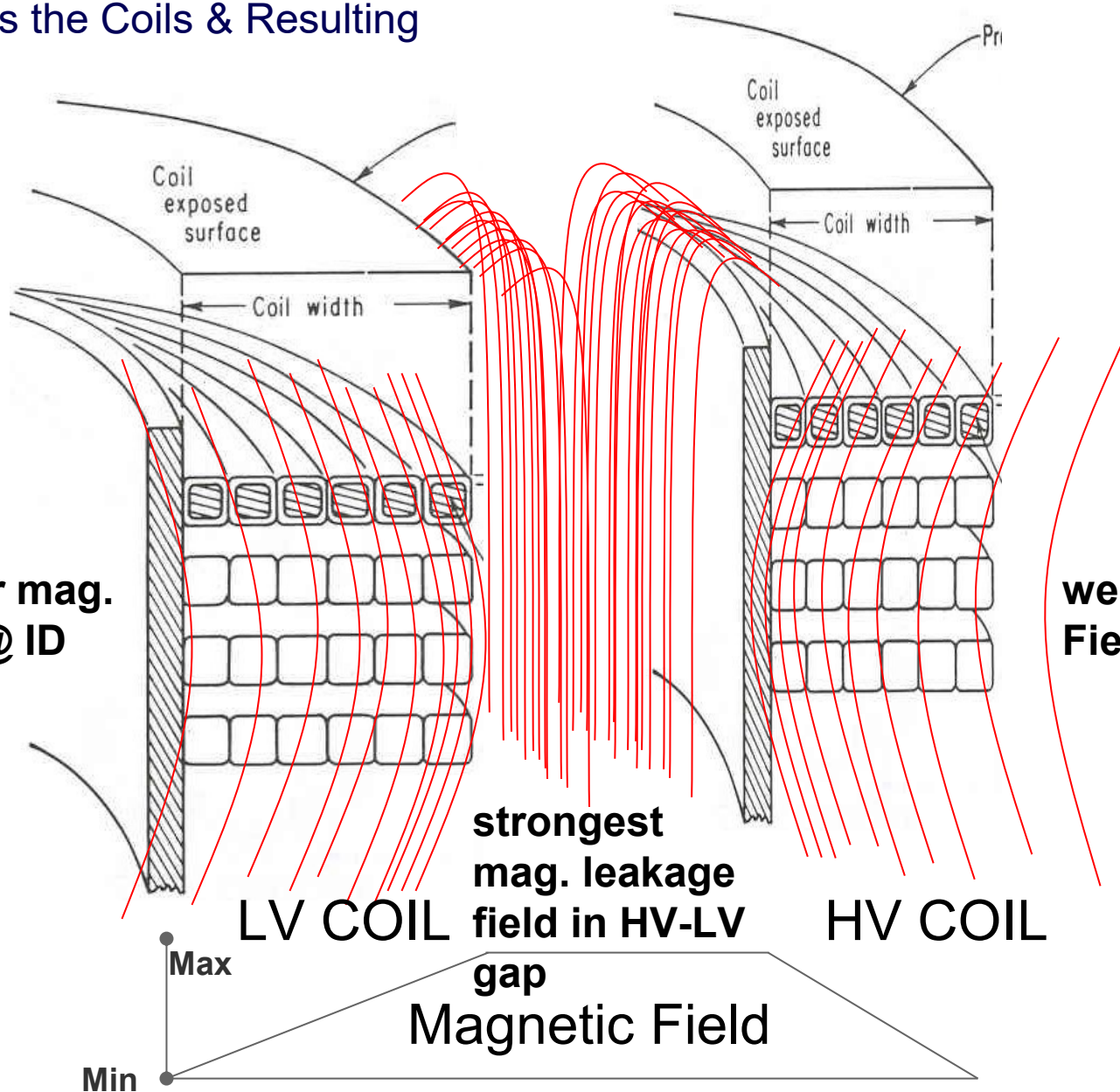
$$F \propto (NI)^2$$

Magnetic “Leakage” Field Across the Coils & Resulting Forces

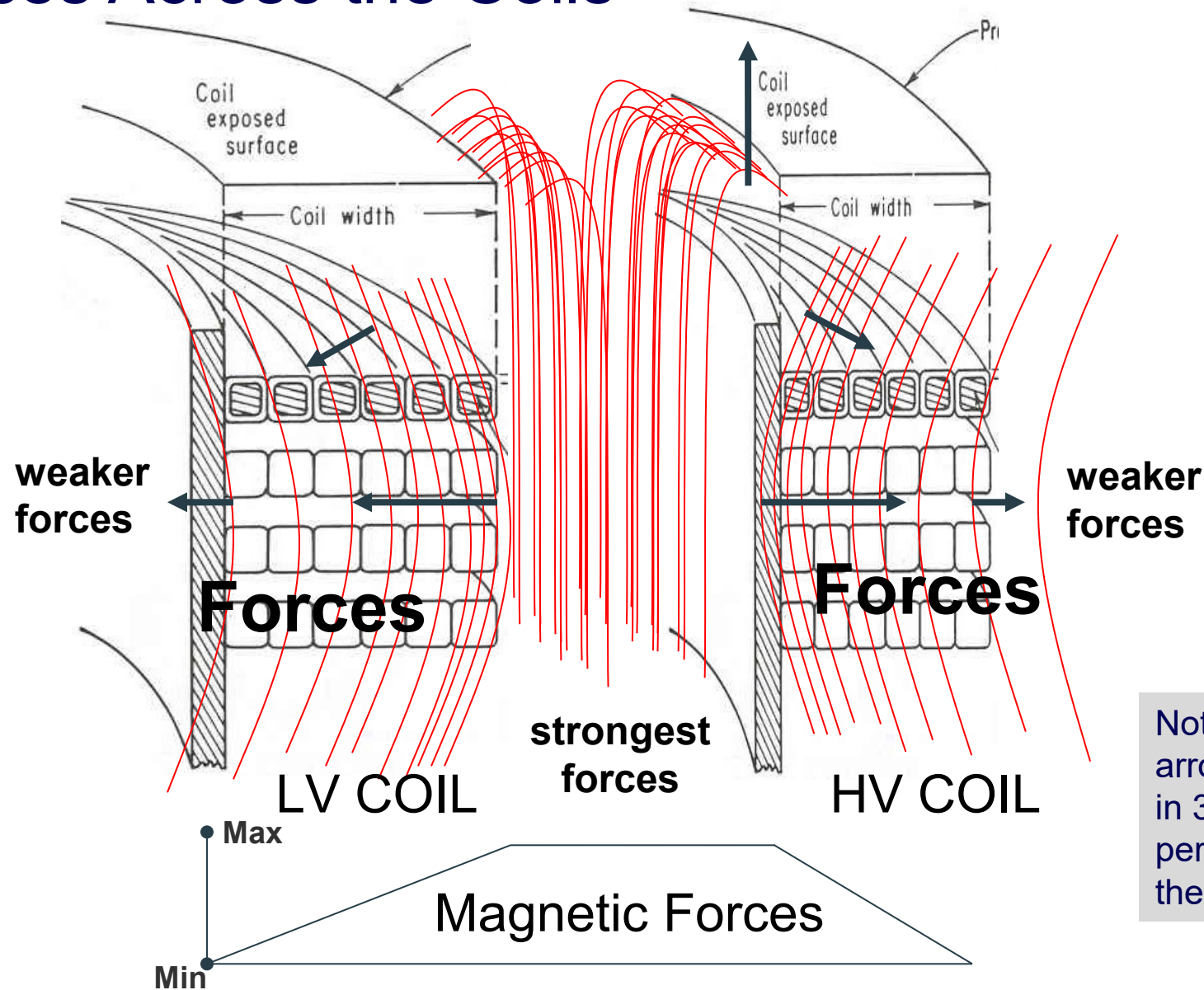
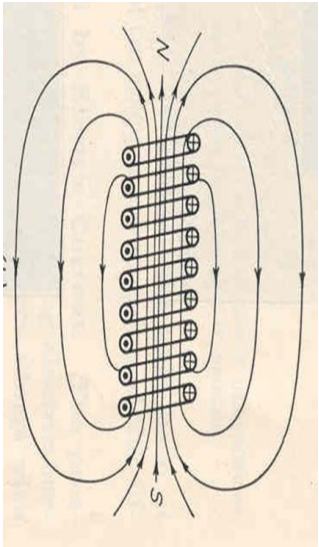
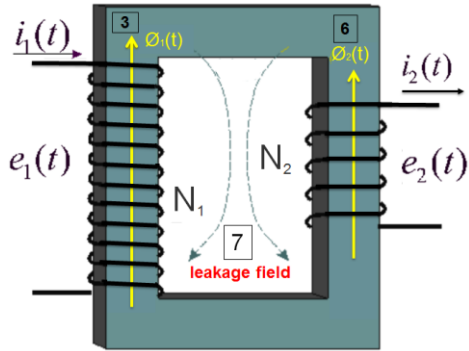


**weaker mag.
Field @ ID**

**weaker mag.
Field @OD**



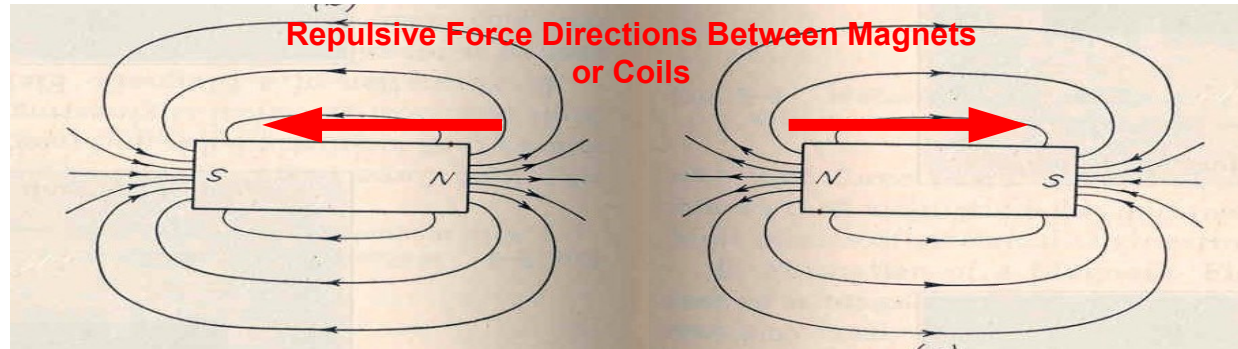
Magnetic Forces Across the Coils



Note: The force arrows are acting in 3-D and perpendicular to the mag fields

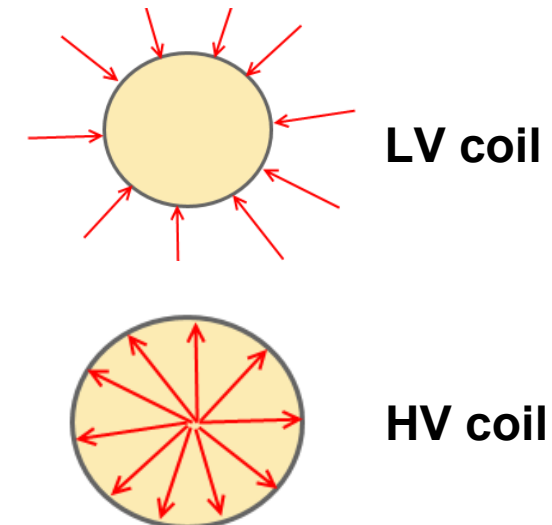
Magnetic Forces

- A net magnetic force also results between two coils (i.e. HV to LV), because the two coils are essentially two huge electro-magnets that repel each other.

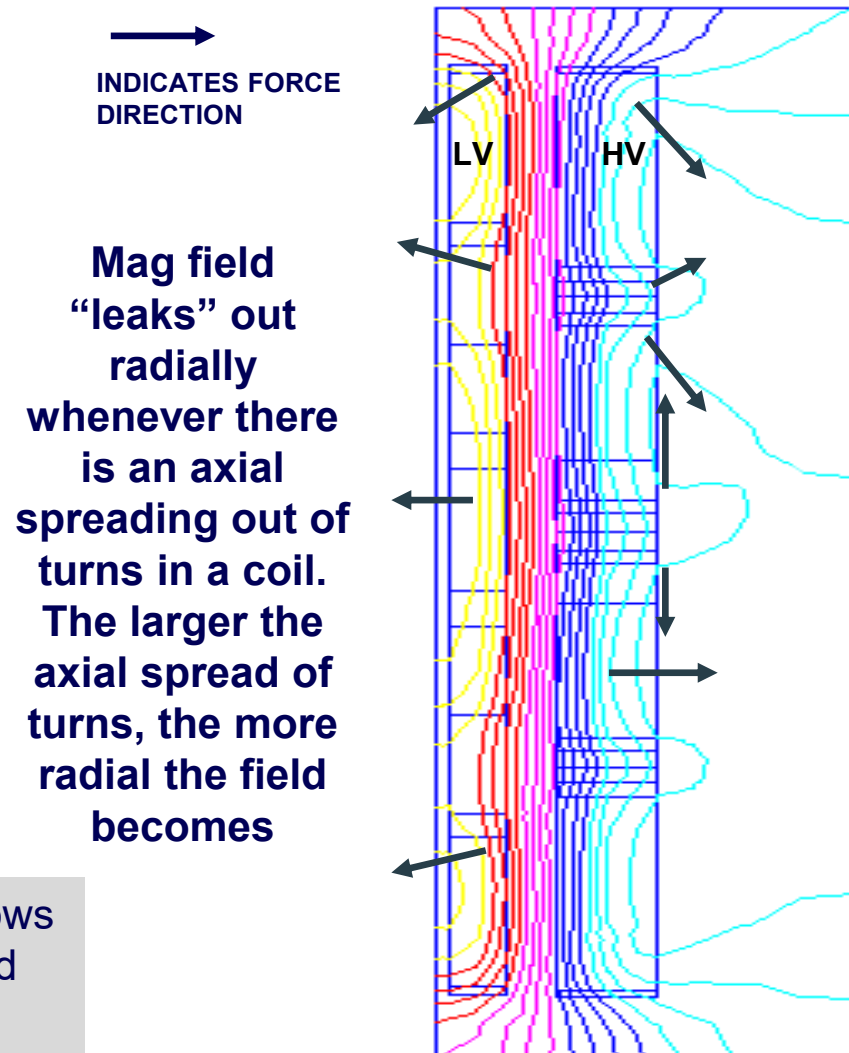


Summative force between these coils could be millions of pounds

- The inner coil experiences net inward radial “crushing” compressive forces
- The outer coil experiences net outward radial expanding type forces

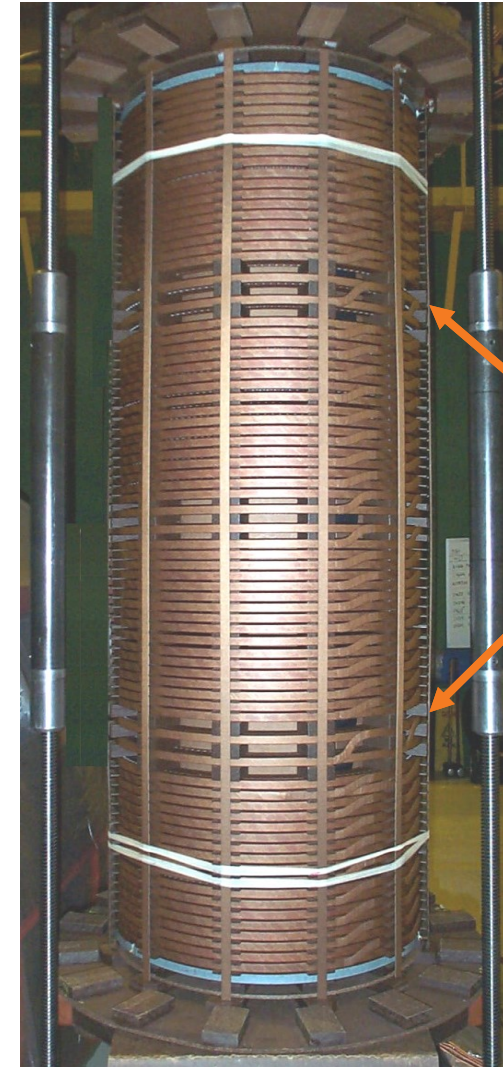


Pictorial of actual FEA field plots



Note: The force arrows
are acting in 3-D and
perpendicular to the
mag fields

Finite Element Analysis of
Leakage Field Between Coils



Axial
locations
of where
HV DETC
taps are
located

Summary of what we discussed so far...

- Magnetic forces are produced whenever
 - You have current flowing thru a conductor, and
 - A leakage magnetic field also passes thru the conductor.
 - Resulting forces have a direction of 90 degrees to the direction of current through the conductor versus the direction of the leakage magnetic field around the conductor (left hand rule)
 - The leakage magnetic fields can pass thru conductors at any angle (3 dimensional)
 - Forces then are also 3 dimensional in nature

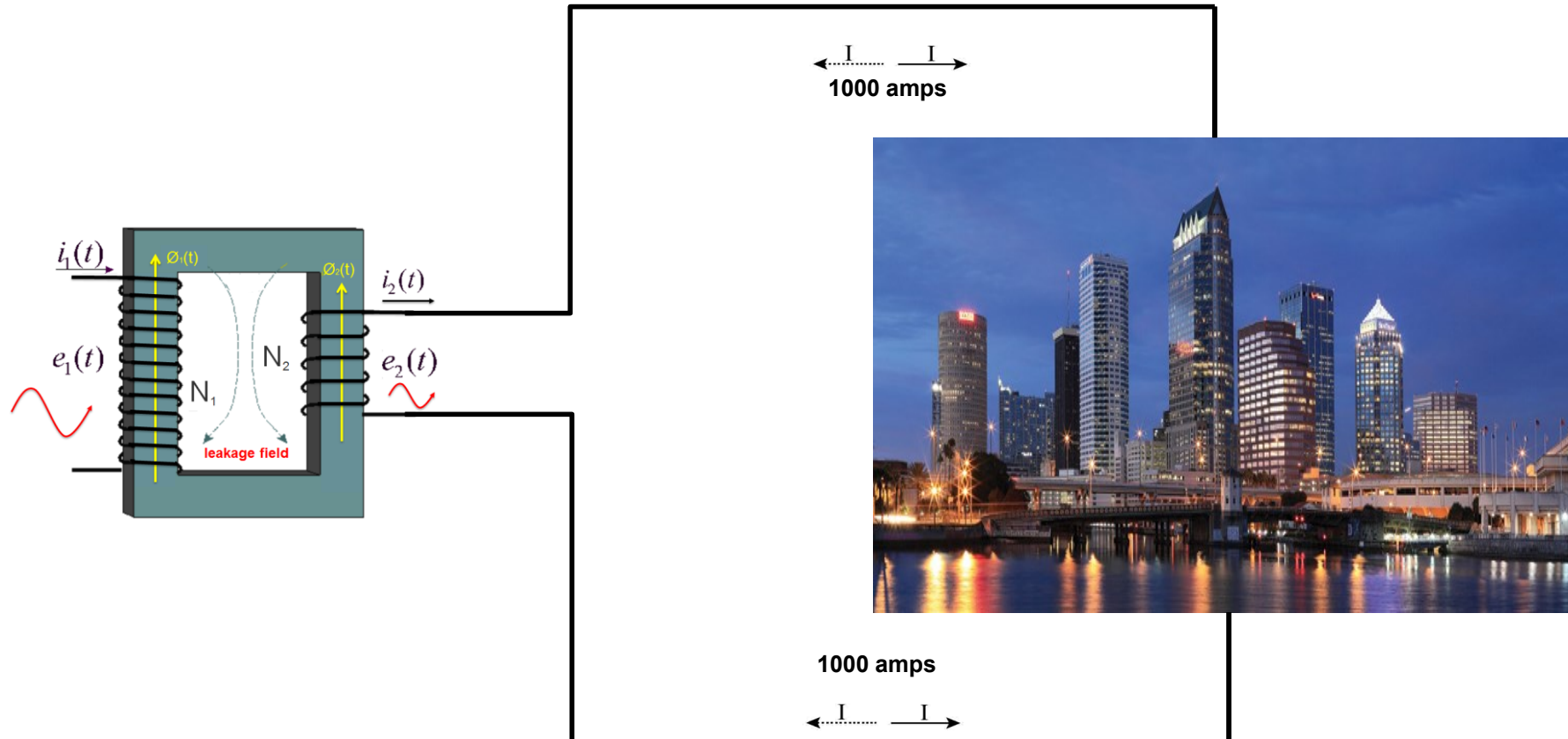
Part 3 – Short Circuits (Faults):

- What are they?
- How do they happen?
- What do they do to my transformer?

Normal Transformer Operation

Normal Circuit

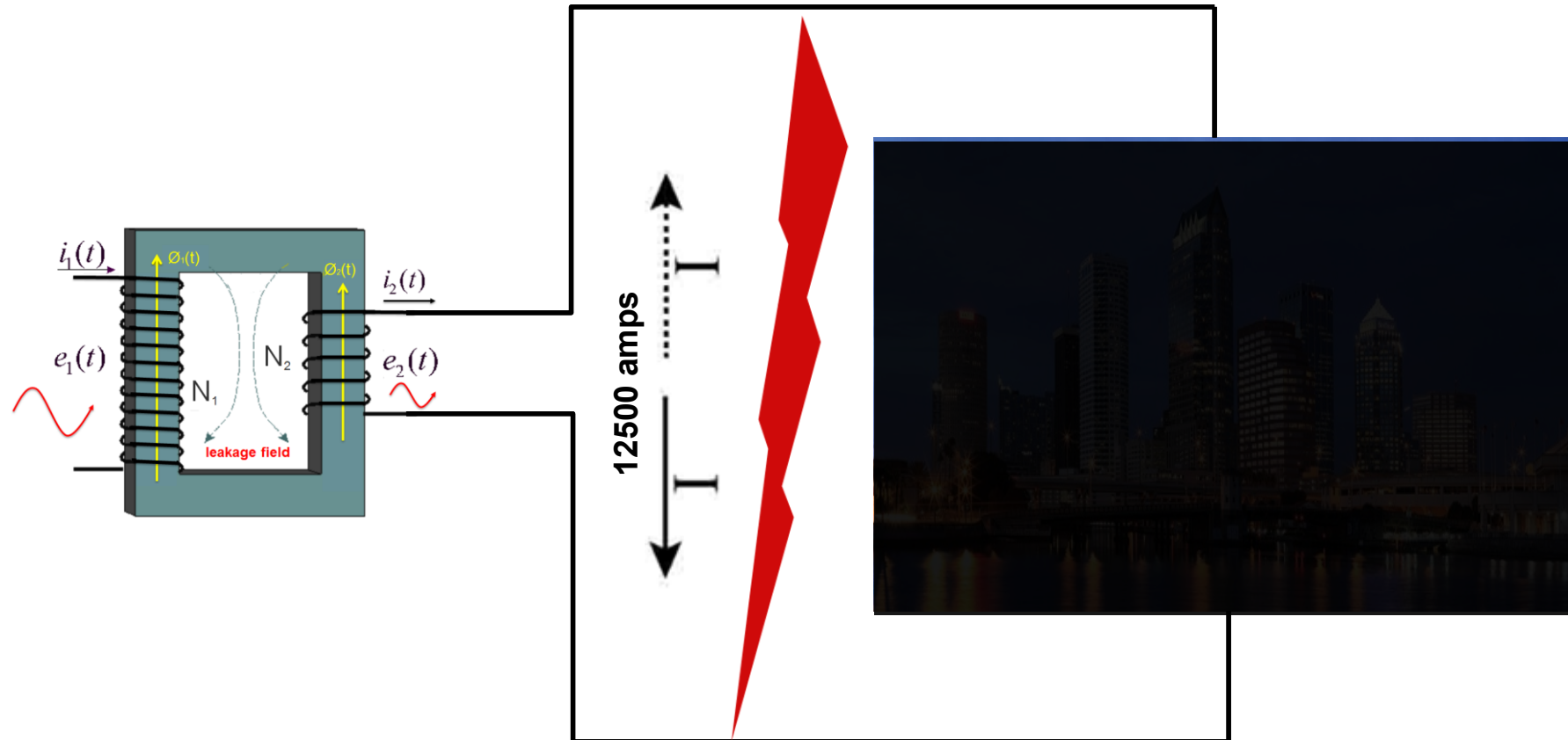
- An AC source supplies power to a given load (i.e. a city). A complete circuit has a source, with power entering a load and returning to the source. Amount of current that flows is directly related to the load on the transformer.



What is a Fault?

System Fault

- An un-intended “electrical connection” made between two energized components having different voltage potentials.
- Results in some (or all) of the current bypassing the intended load.
- Currents are typically very high due to low “fault impedance”



Types of Faults (and how they happen)

Basic Types of Faults in Power Systems

- Line-to-Ground (Most Common)
 - One or more conductors make “electrical” contact to ground
 - Example: Wildlife or Lightning. A lightning strike hits a line, then causes a flashover. The stroke between the line and ground causes ionization of the air (a conductive channel path to ground).



Lightning can reach 100 million to 1 billion volts, and generate up to a billion watts of power

Types of Faults (*cont.*)

Basic Types of Faults in Power Systems

- Line-to-Line
 - Two different phases come into direct or indirect contact with each other
 - Example: A bird with a large wingspan touches two conductors simultaneously and creates a conductive path between the two lines



Types of Faults (*cont.*)

Basic Types of Faults in Power Systems

- Double Line-to-ground
- Three Phase (least common)
 - Similar to Line-to-Line but when all three phases make contact with each other
 - Example: A falling tree on a transmission line creates a conductive path between all 3 lines and to ground



Designing For Short Circuit

Section 7 of IEEE C57.12.00 addresses design requirements for short circuit

- Fault current magnitudes and their behavior over time (time durations, wave shapes, etc).
- Temperature limits of winding conductor after a fault
- Power system impedance that may be used to help limit fault current
- Short circuit test methods and how to analyze, inspect, etc.

Example of How to Calculate SC Current

C57.12.00 Section 7 defines both symmetrical and asymmetrical current

Symmetrical Current

$$I_{SC} = \frac{I_R}{Z_T + Z_S}$$

- I_{sc} – symmetrical SC Current (A, rms)
- I_r – rated current (A, rms)
- Z_t – transformer impedance for same voltage tap and MVA as rated current (I_r)
- Z_s – system impedance in per unit on the same MVA base for rated current (I_r)

Asymmetrical Current

$$I_{SC}(pk\ asym) = K I_{SC}$$

$$K = \left\{ 1 + \left[e^{-\left(\phi + \frac{\pi}{2}\right) \frac{r}{x}} \right] \sin \phi \right\} \sqrt{2}$$

ϕ is arc tan (x/r) (radians)

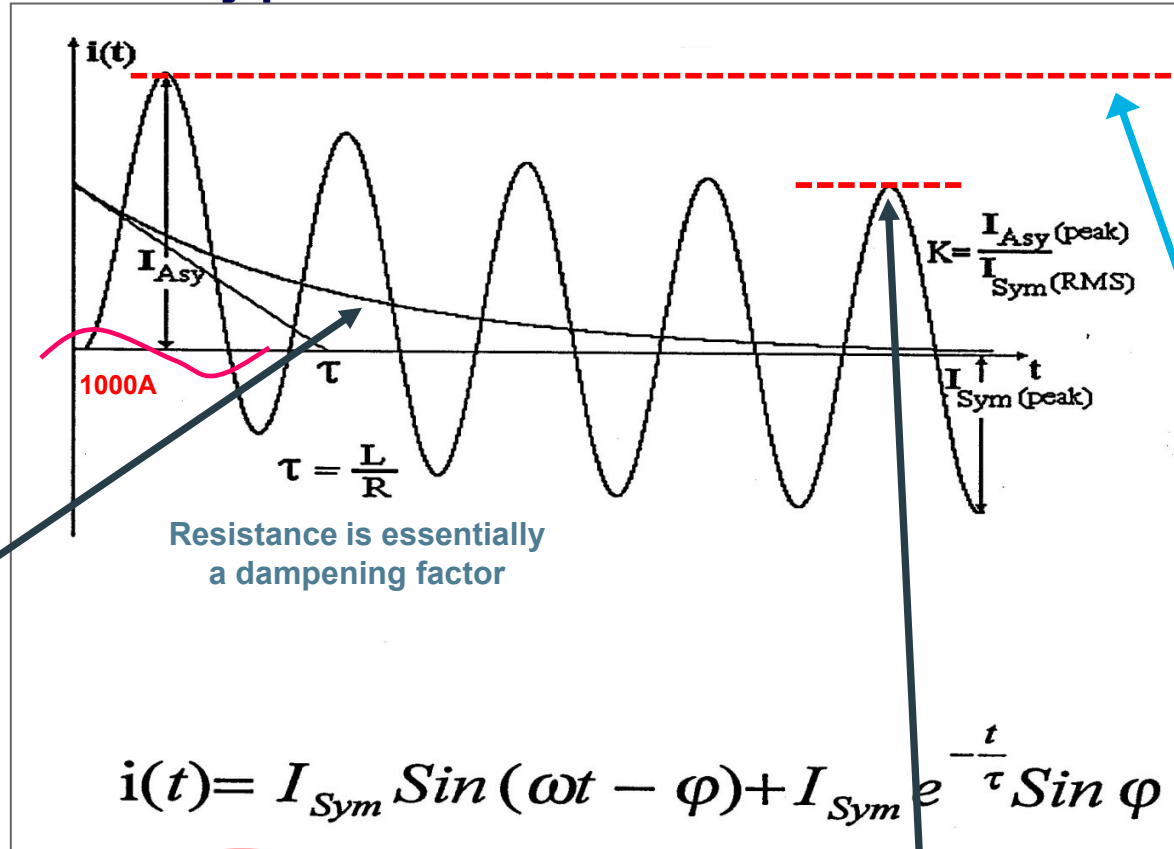
e is the base of natural logarithm

x/r is the ratio of effective ac reactance to resistance, both in ohms

Waveform of Typical Fault Current Over Time

(Symmetrical and Asymmetrical)

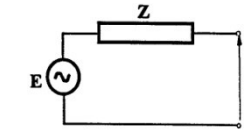
The fault current within a transformer will follow this typical exponential decay



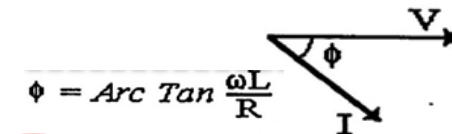
Symmetrical (RMS) current

Say Z were to be 8.0%, then:
Isc would be 12.5x normal rated current

$$I_{SC} = \frac{I_R}{\frac{Z_T + Z_S^*}{100}} \quad \text{OR} \quad I_{SC} = \frac{100}{\%Z} \times I_R$$



$$Z(pu) = \frac{MVA_{Trans}}{MVA_{S/C}}$$



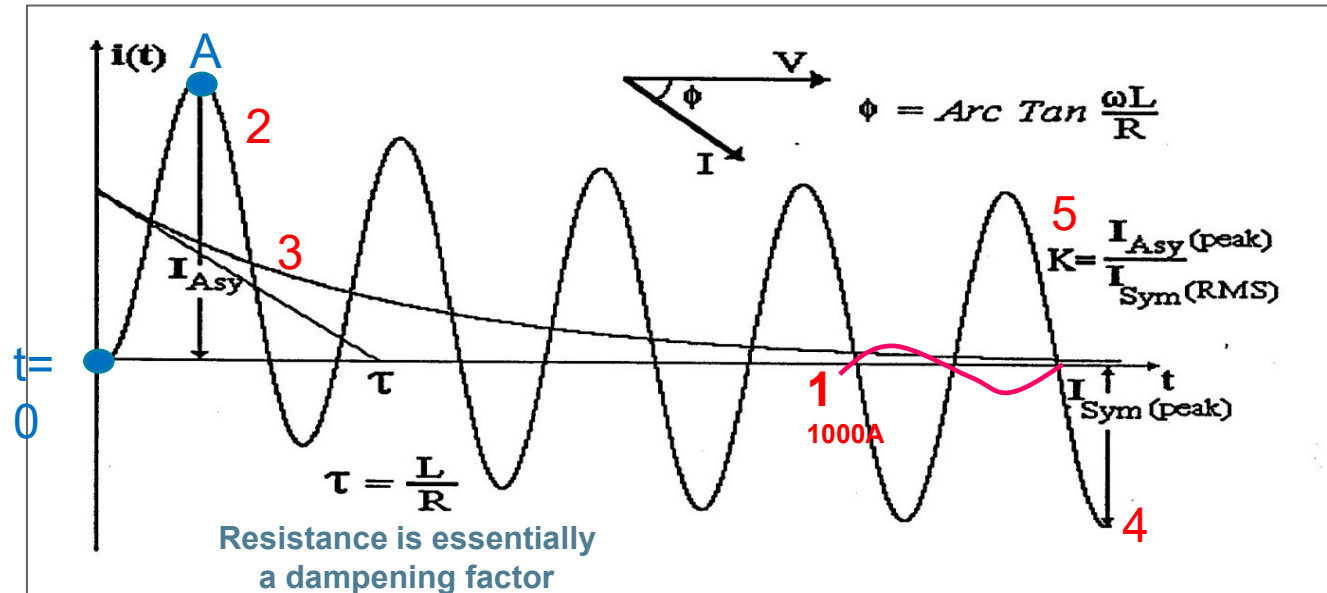
Asymmetrical (Peak) current

$$I_{SC} (peak \text{ asym}) = K I_{SC} \text{ where}$$

$$K = \left\{ 1 + e^{-\left(\phi + \frac{\pi}{2}\right) \frac{r}{x} \sin \phi} \right\} \sqrt{2}, \text{ per unit}$$

$$\phi = \arctan \frac{x}{r}, \text{ radians}$$

Different Parts of the Formulas...



1 – Rated current

2 – Asymmetrical current

Total fault current includes symmetrical and asymmetrical components

3 – Asymmetrical decay

Decay is an exponential function

4 – Symmetrical current

Function of rated current and impedance

5 – Asymmetry factor

Formula will calculate first asymmetrical peak – point A

Offset K factor ranges from 1.51 – 2.83, mainly dependent on x/r ratio

Convert from RMS to peak w $\sqrt{2}$

To find the current at any point in time

$$i(t) = I_{\text{Sym}} \sin(\omega t - \phi) + I_{\text{Sym}} e^{-\frac{t}{\tau}} \sin \phi$$

$$I_{\text{SC}} = \frac{I_R}{Z_T + Z_S} \quad \text{OR} \quad I_{\text{SC}} = \frac{100}{\%Z} \times I_R$$

$$I_{\text{SC (peak asym)}} = K I_{\text{SC}} \quad \text{where}$$

$$K = \left\{ 1 + e^{-\left(\phi + \frac{\pi}{2}\right) \frac{r}{x} \sin \phi} \right\} \sqrt{2}, \text{ per unit}$$

$$\phi = \arctan \frac{x}{r}, \text{ radians}$$

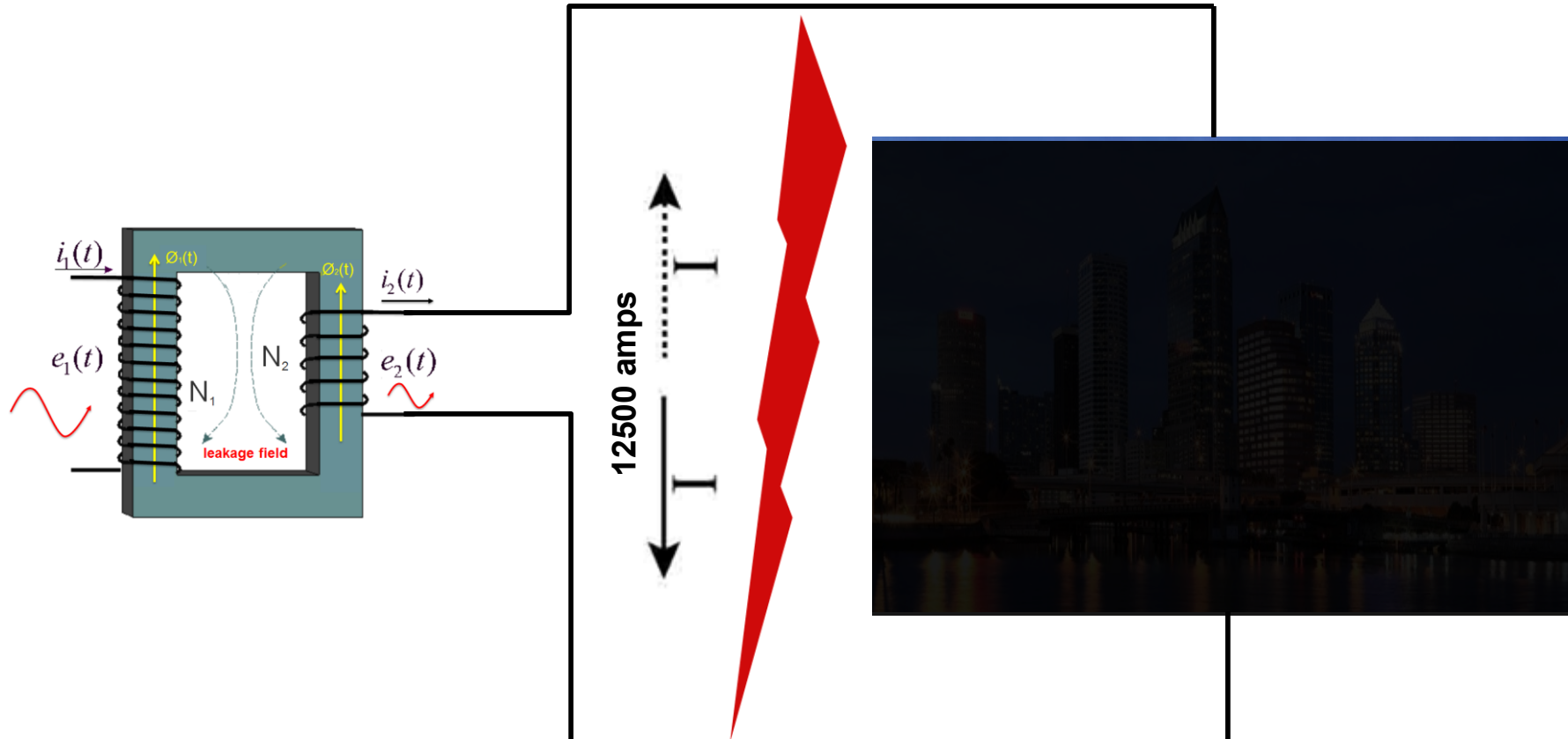
Part 4 – Visualization of the Magnetic Forces:

- Axial Forces on Winding Conductors (and other components)
- Radial Forces on Winding Conductors
- Combination of Axial/Radial Forces

Back to our Fault Condition...

System Fault

- An un-intended “electrical connection” made between two energized components having different voltage potentials.
- Results in some (or all) of the current bypassing the intended load.
- Currents are typically very high due to low “fault impedance”



Once the Fault Occurs...

- The transformer must source the current to feed the fault
- Very high currents (much higher than rated current) begin to flow in the transformer windings
- Very high temperatures can be generated in the winding conductors and paper insulation resulting from the high currents that flow.
- Very high magnetic forces can be generated within windings, leads, supporting structures and insulation systems.

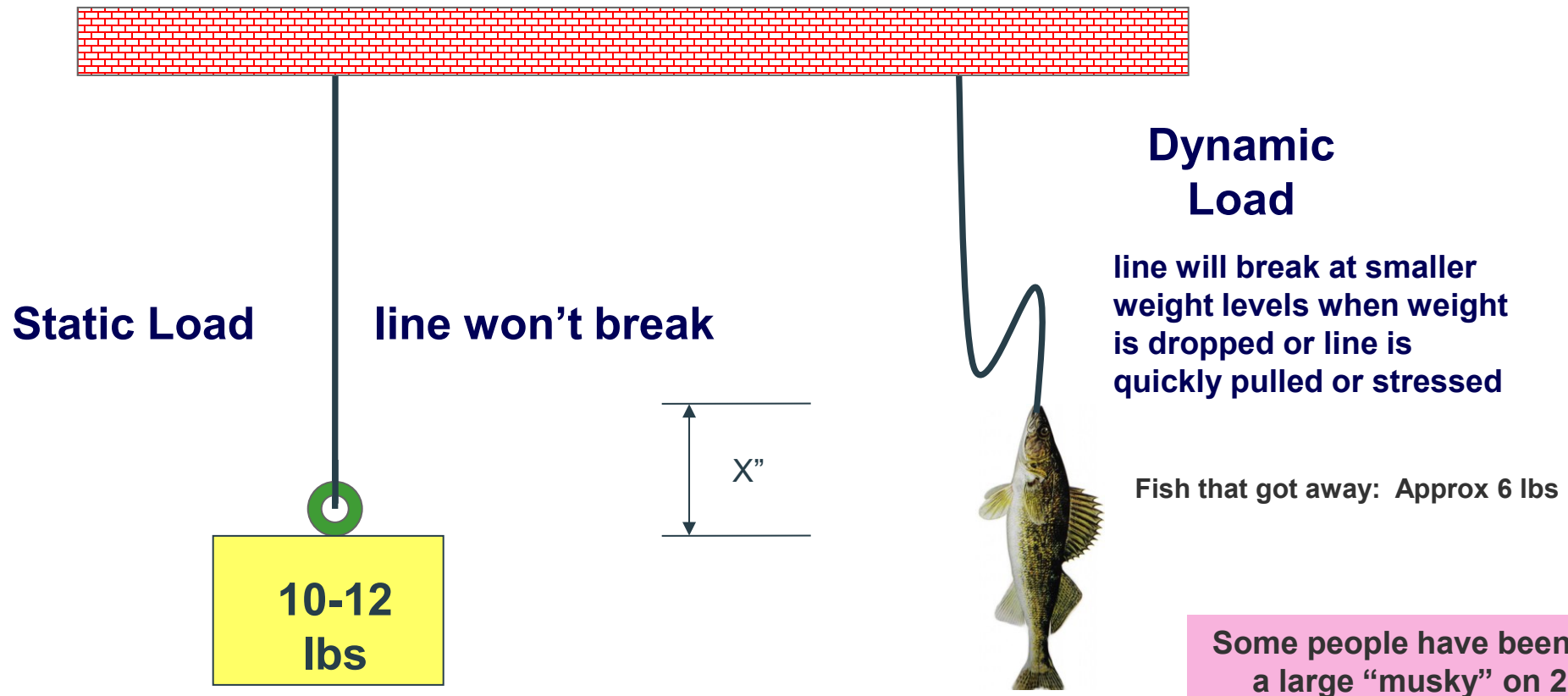
Short circuit forces are all acting in 3-D
(combination of axial/radial/angular).

They can reach summative levels of up to 2+ million lbs,
per phase, **INSTANTANEOUSLY!**

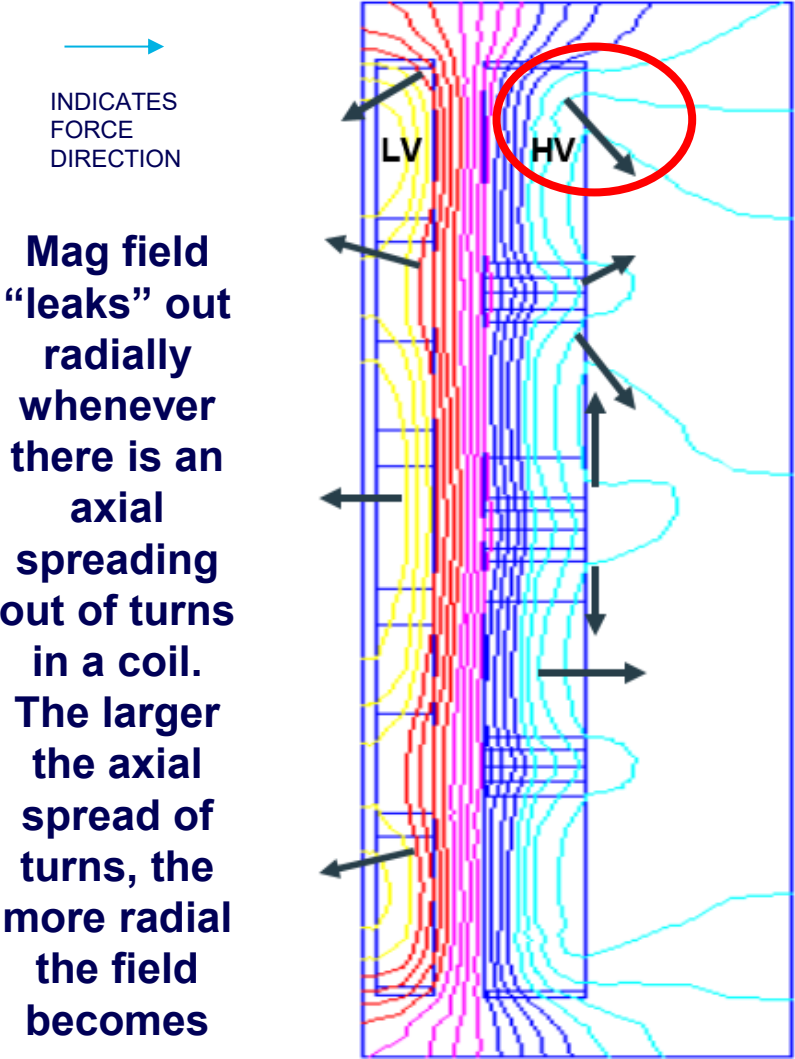
Physics of Materials: Static vs Dynamic Stress

We know that: All materials behave differently under static (stationary) versus dynamic (moving) load conditions

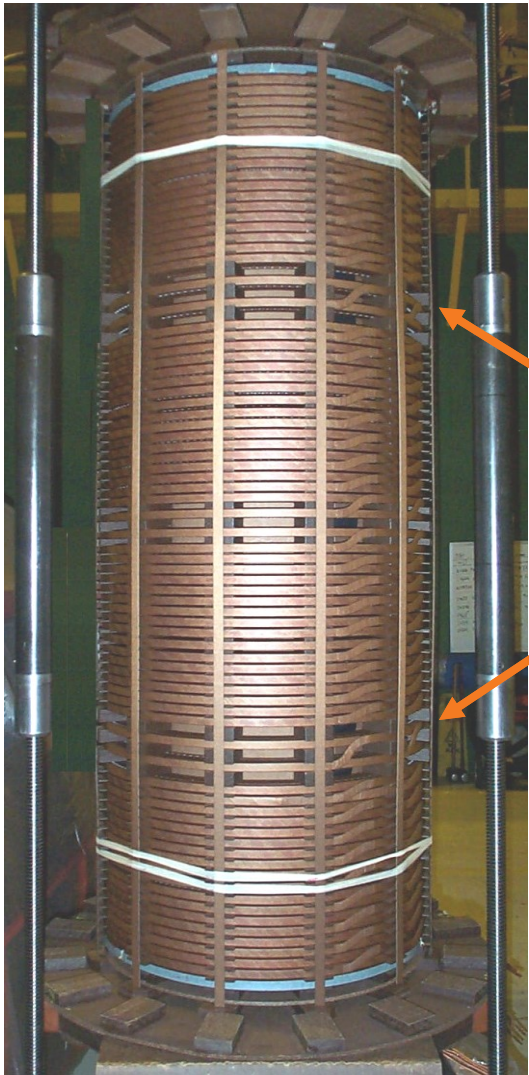
Example using a weight suspended from a 10 lb test fishing line



Visualization of Magnetic Fields and Forces

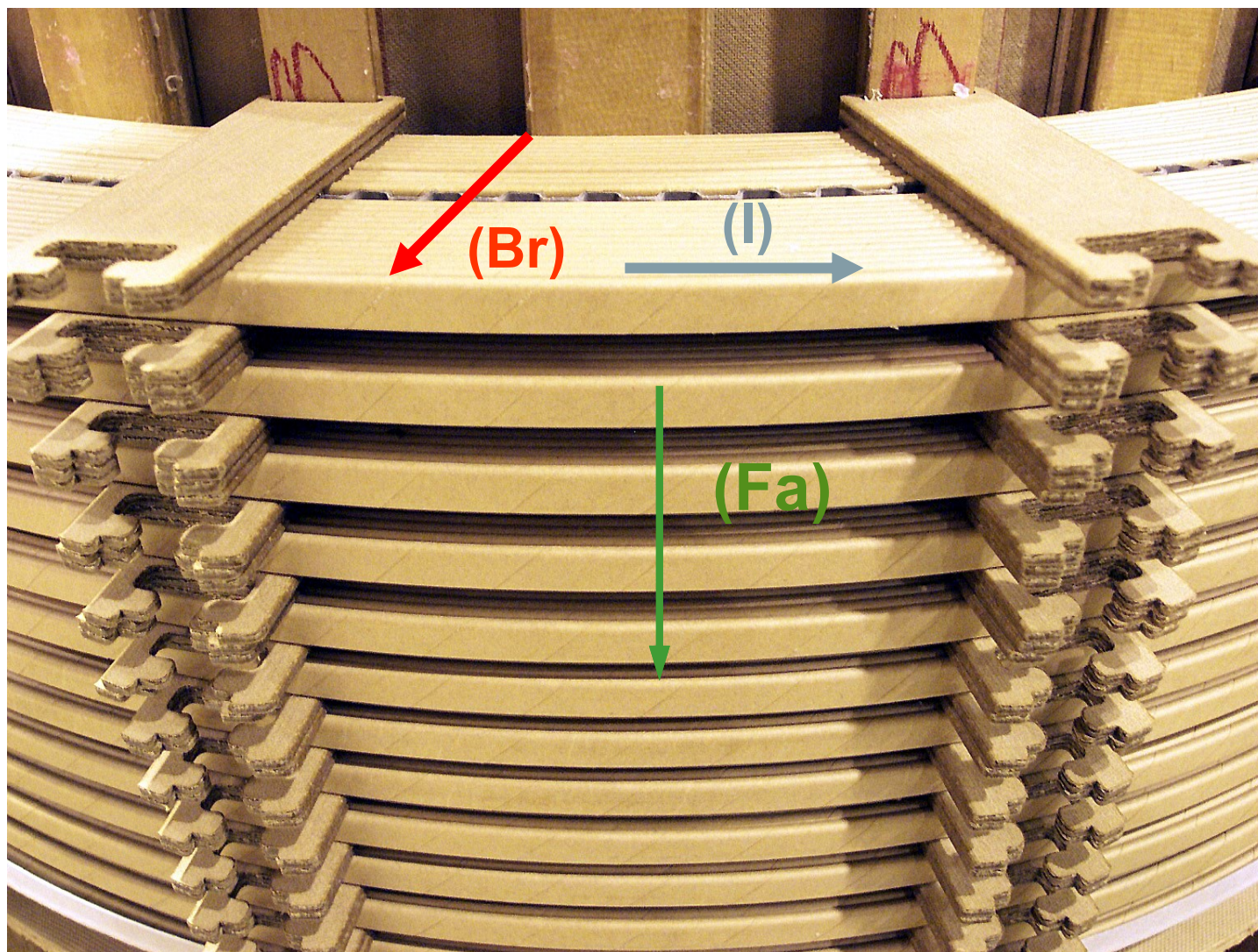


**Finite Element Analysis of
Leakage Flux Between Coils**



**Axial
locations of
where HV
DETC taps
are located**

Axial Forces - (Applying Left Hand Rule)



Current (I)

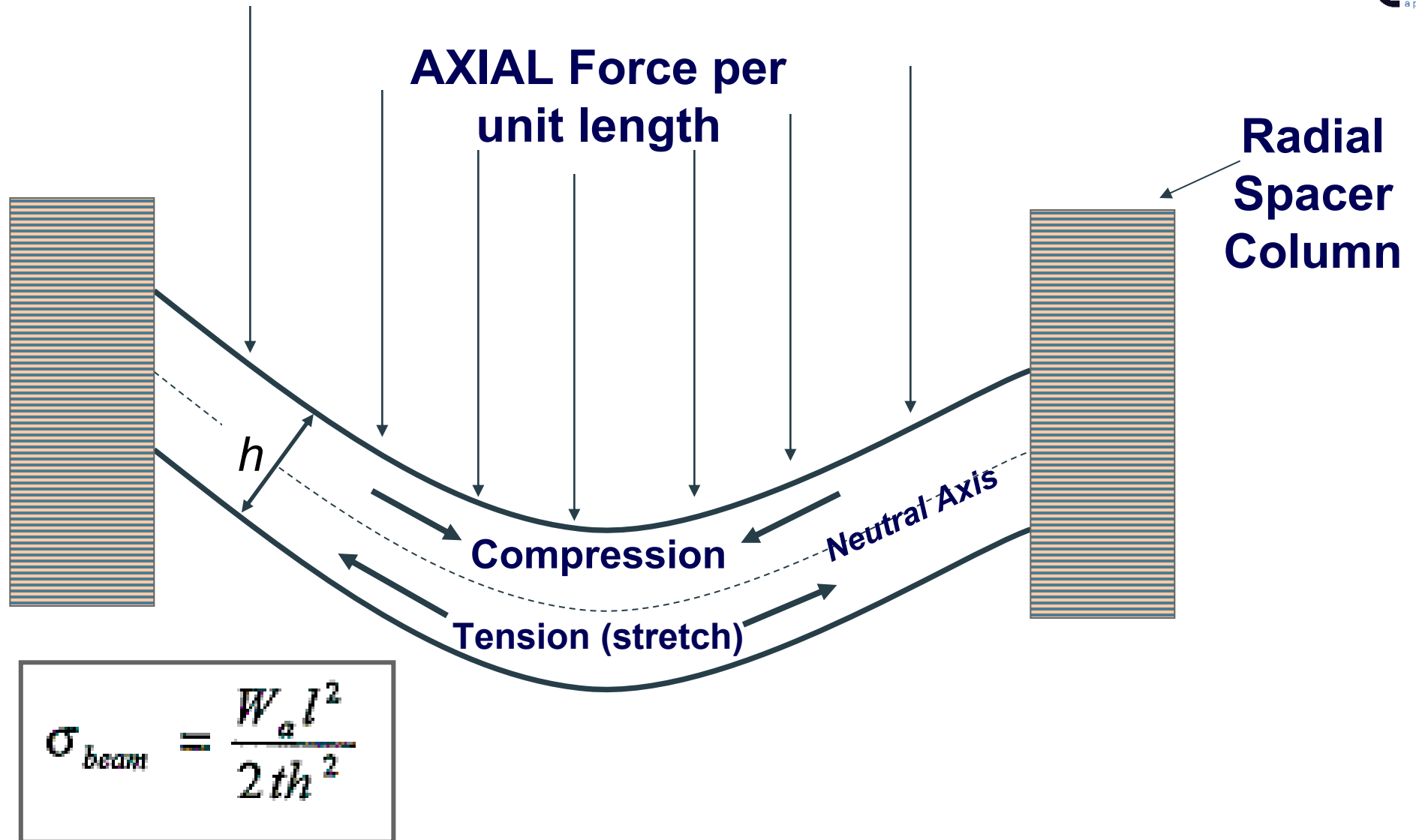
Flux (B)

Force (F)

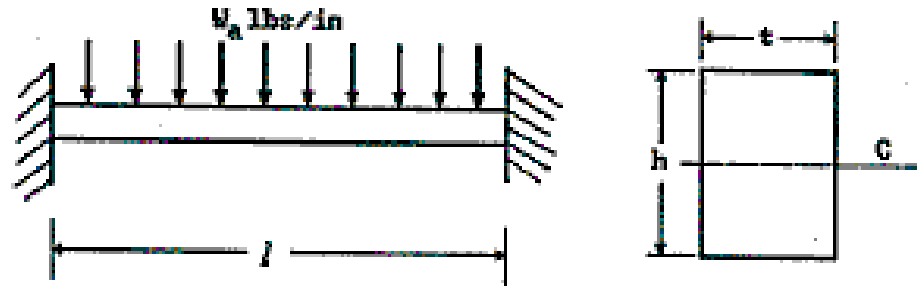
Length of beam:

$$l = \frac{2 \pi R_{od}}{m} - W_b$$

Beam Bending Under Load (elevation view)



Beam Bending Stress



$$\sigma_{beam} = \frac{W_a l^2}{2 t h^2}$$

where:

R_{OD} = Winding O.D. (inches)

W_k = Keyspacer Width (inches)

m = Number of Key Spacer Strings

F_{max} = Maximum Force on a Disk or Conductor (lbs)

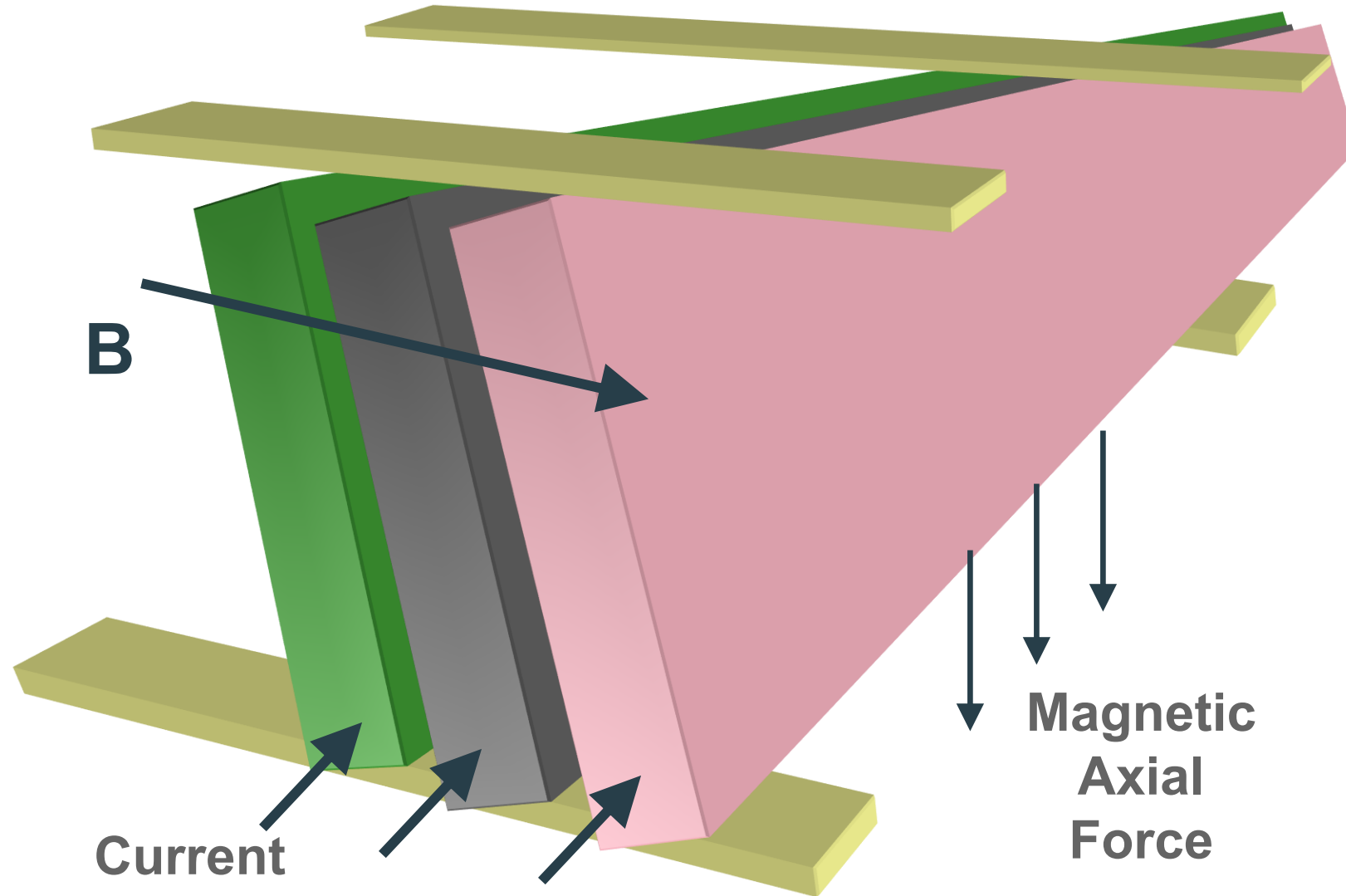
Length of beam:

$$l = \frac{2 \pi R_{OD}}{m} - W_k$$

Linear Load:

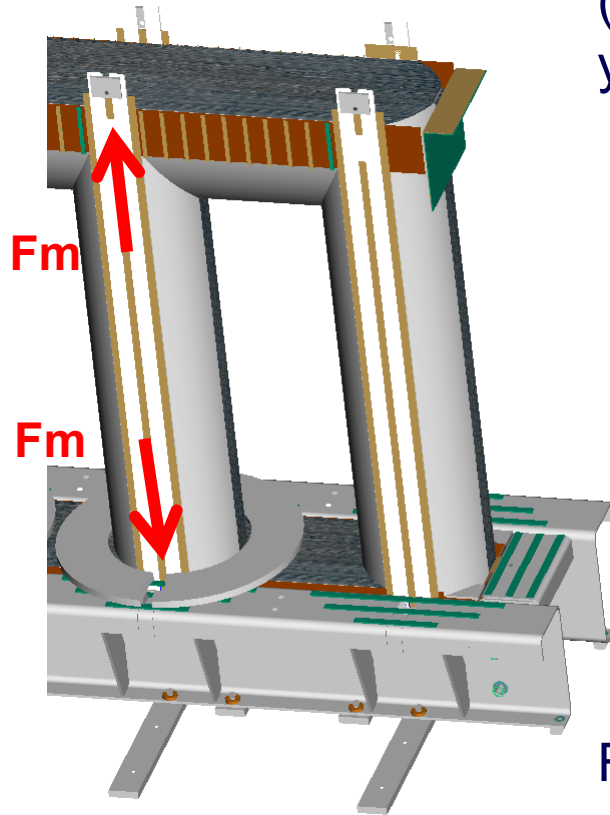
$$W_a = \frac{F_{max}}{l}$$

Conductor Tipping/Tilting



Stress in Tie Bars (Verticals)

The minimum cross-sectional area of the tie bar (A_{tb}) is determined by the force applied and the yield point of the tie bar material.



$$A_{tb} = \frac{F_m/2}{70,000}$$

Yield Strength of Tie Bar = 100,000 PSI

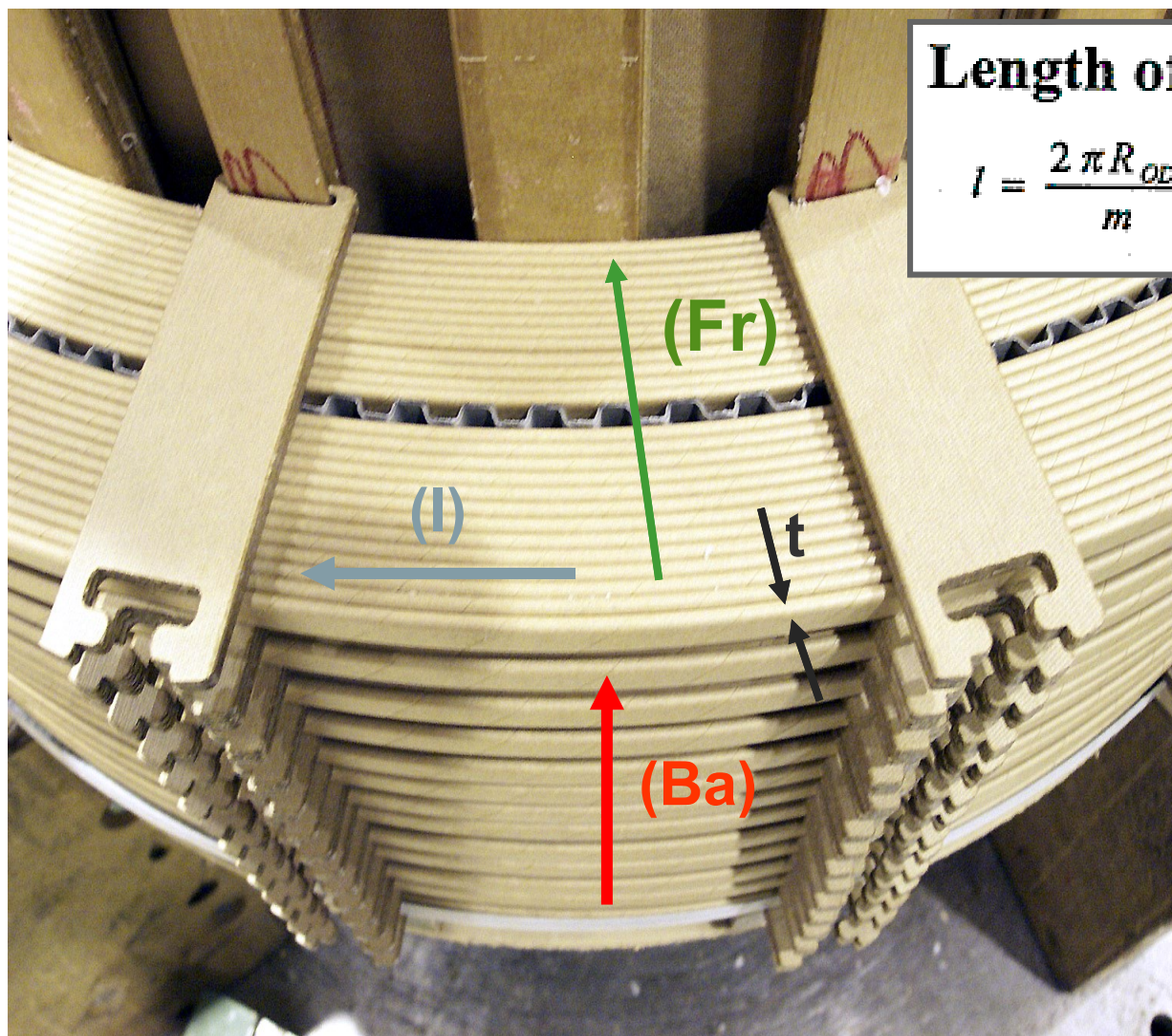
70% of yield = 70,000 PSI

$F_m/2$ to get minimum area per tie bar (2 per phase)

F_m is the larger of:

- maximum axial short circuit force (PSI)
- maximum winding sizing per phase (PSI)

(Inward) Radial Forces – Buckling (inner coil)



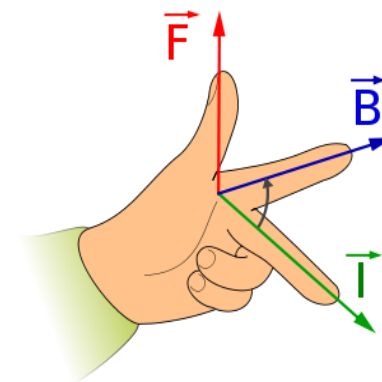
Length of beam:

$$l = \frac{2 \pi R_{OD}}{m} - W_{kr}$$

Current (I)

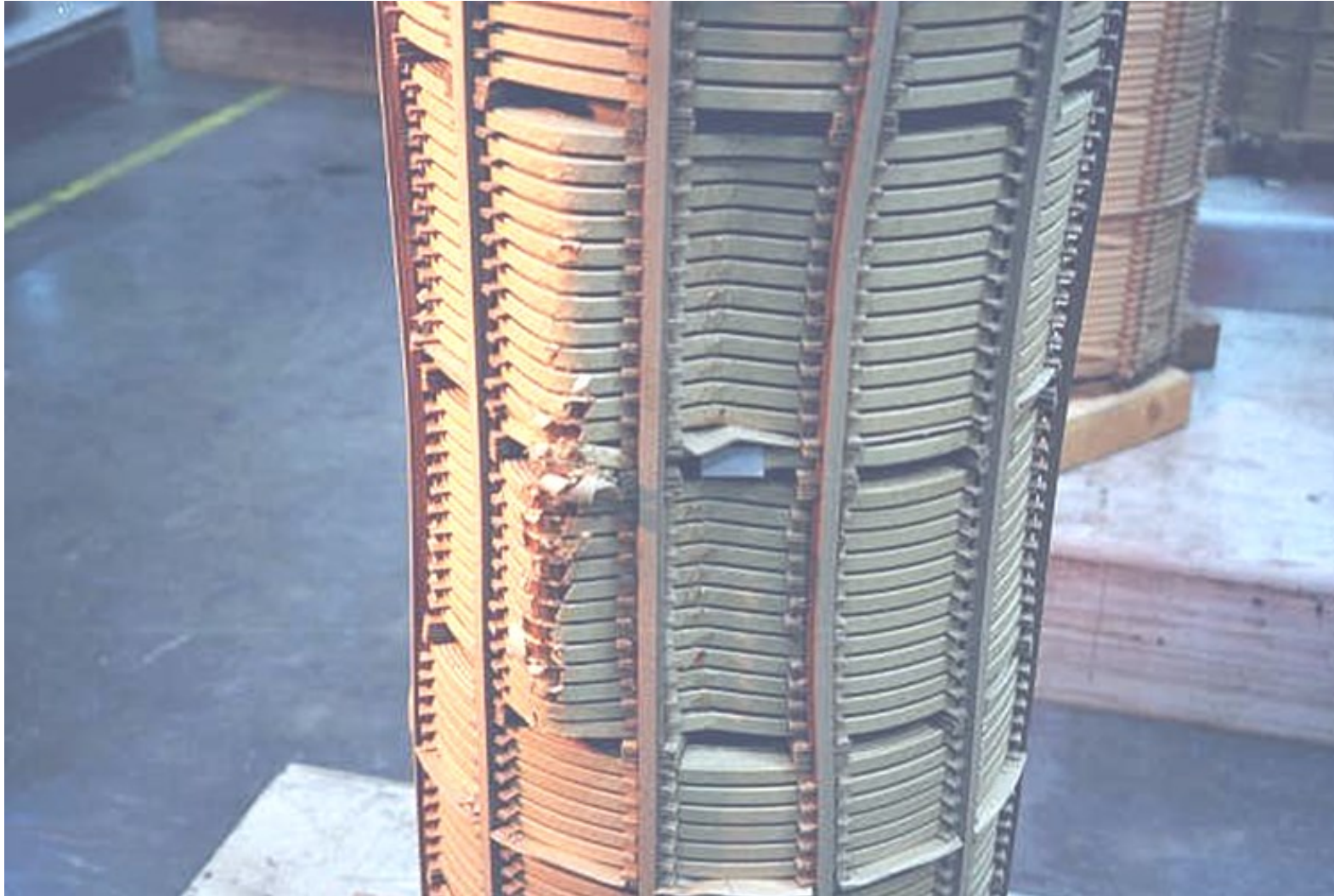
Flux (B)

Force (F)

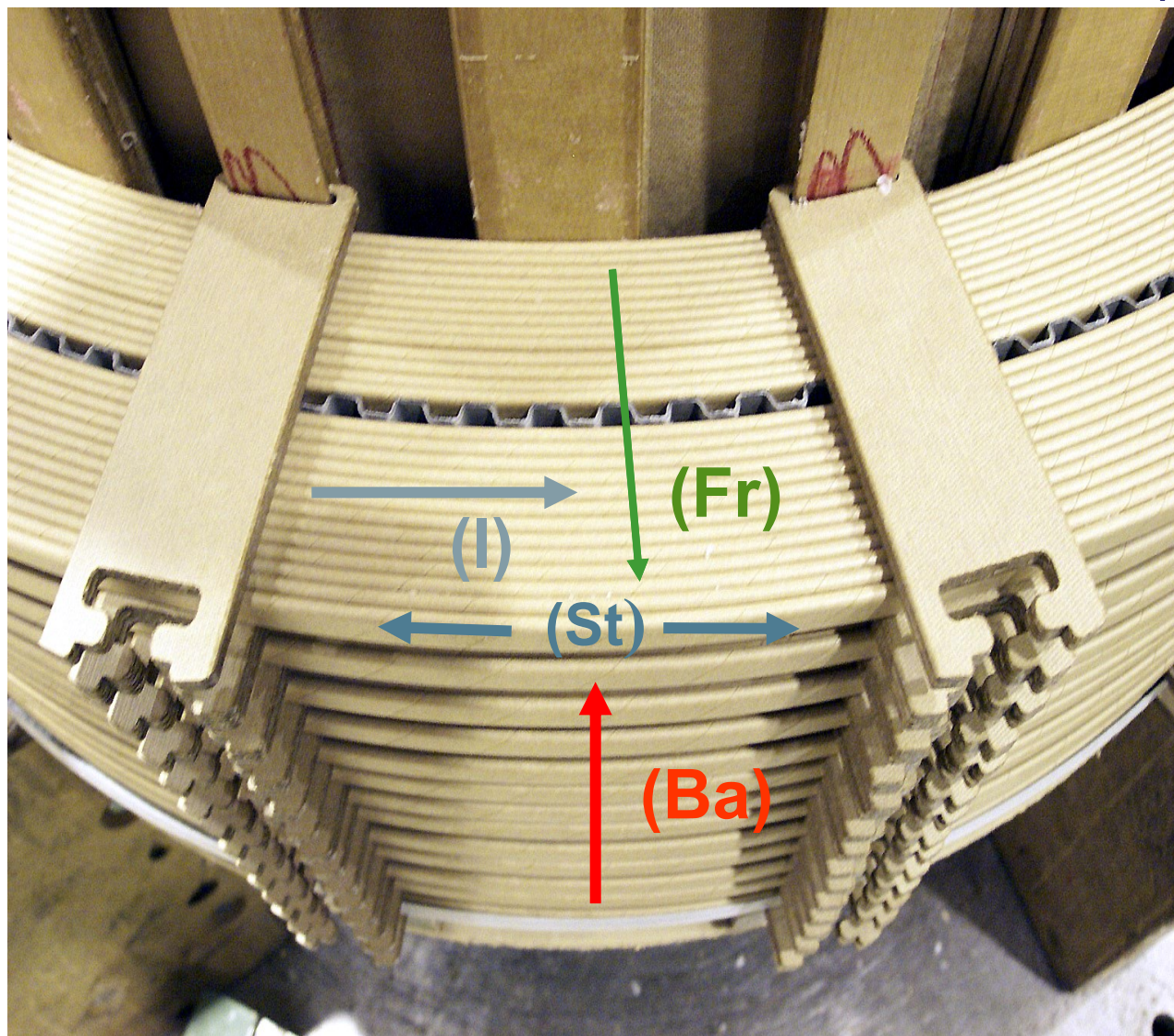


Left-Hand Rule

Buckling Photo - Inner Winding Forced Into Failure in a Laboratory Setting...



OUTWARD Radial Forces – Hoop Stress (outer coil)

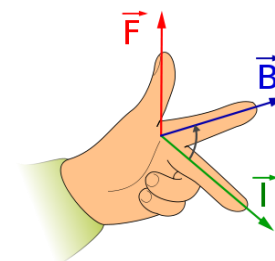


Current (I)

Flux (B)

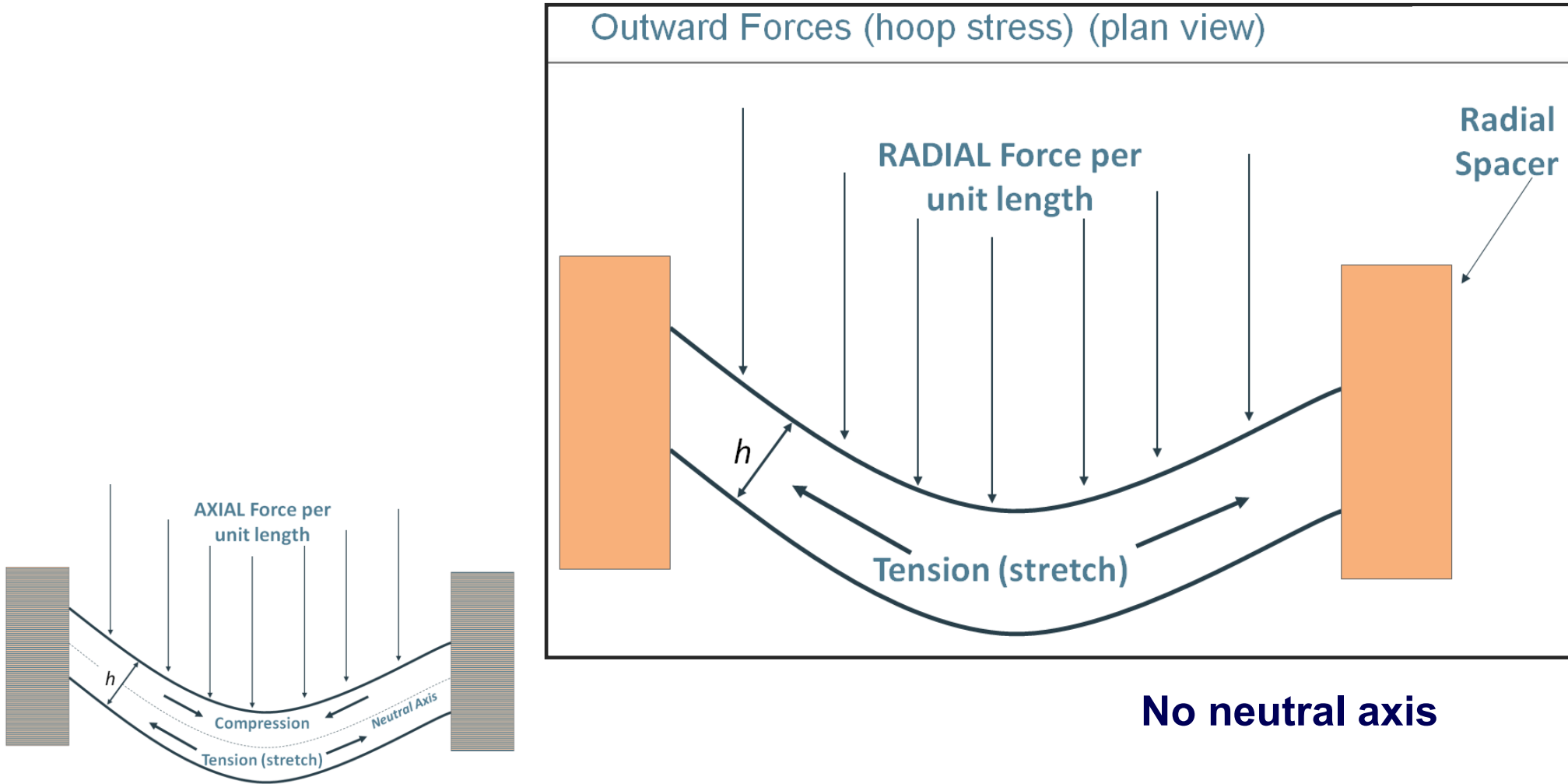
Force (F)

Tensile
Stress (St)



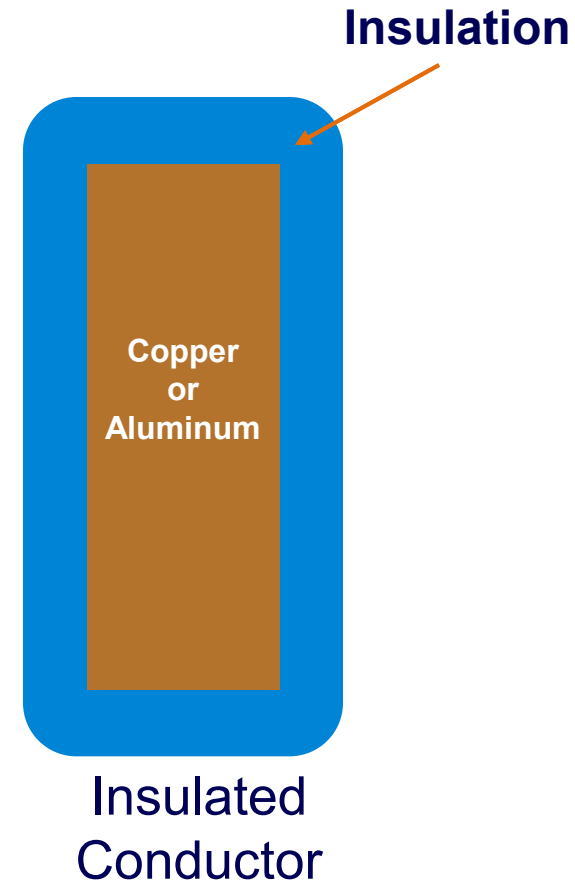
Left-Hand Rule

Outward Forces (hoop stress) - Outward Radial Force exerts Tensile Stress only



Winding Temperature During a Short Circuit

- Calculated on basis that all heat is stored (heats up too quickly to radiate heat to equilibrium)
- Temperature not to exceed
 - 250°C for copper
 - 200°C for EC grade aluminum
- Method defined on IEEE C57.12.00-2000 section 7.4.



Winding Temperature During a Short Circuit

Approximate method:

$$T_f = \frac{(S_{\Delta k})^2 t}{K_m} + T_{OR} + T_a$$

T_f = final winding temperature at end of a short circuit (°C)

T_{OR} = maximum top liquid temperature rise over ambient temperature (°C)

T_a = ambient temperature (°C)

$S_{\Delta k}$ = winding current density at symmetrical short circuit current (W/dm²)

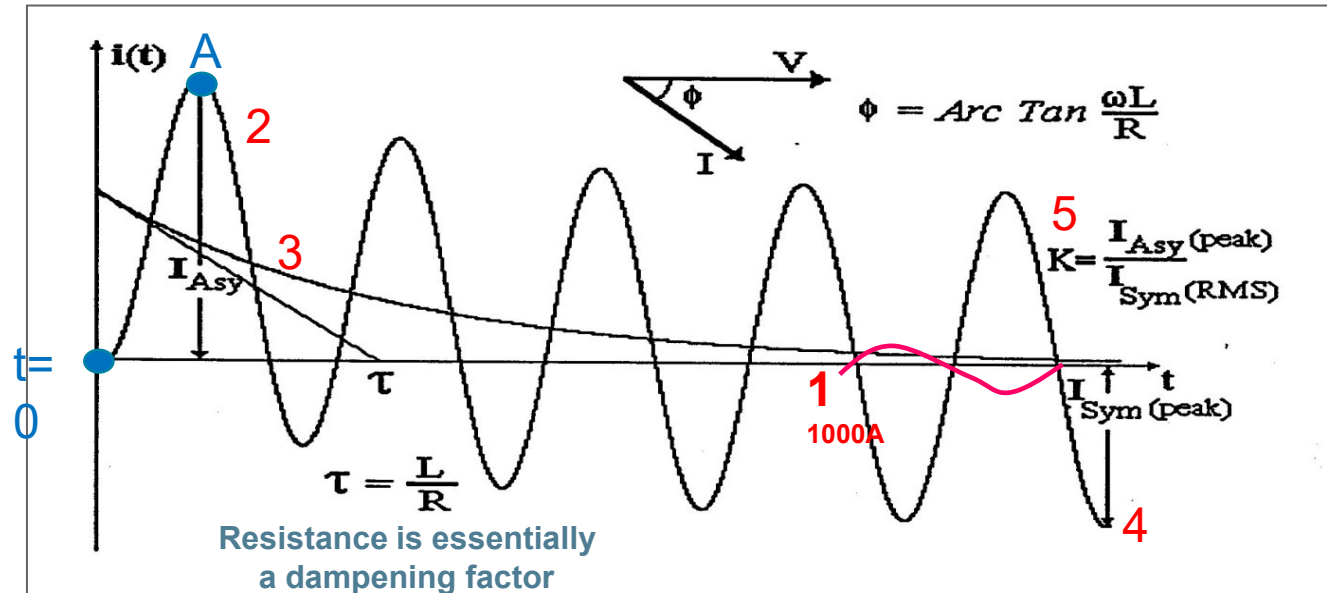
t = short circuit duration (s).

K_m = 156 for copper / 73 for EC grade aluminum

Part 5 – Calculation Example:

- Calculate short circuit current and asymmetrical offset factor

Back to our formulas again....



1 – Rated current

2 – Asymmetrical current

Total fault current includes symmetrical and asymmetrical components

3 – Asymmetrical decay

Decay is an exponential function

4 – Symmetrical current

Function of rated current and impedance

5 – Asymmetry factor

Formula will calculate first asymmetrical peak – point A

Offset K factor ranges from 1.51 – 2.83, mainly dependent on x/r ratio

Convert from RMS to peak w $\sqrt{2}$

To find the current at any point in time

$$i(t) = I_{\text{Sym}} \sin(\omega t - \phi) + I_{\text{Sym}} e^{-\frac{t}{\tau}} \sin \phi$$

$$I_{\text{SC}} = \frac{I_R}{Z_T + Z_S} \quad \text{OR} \quad I_{\text{SC}} = \frac{100}{\%Z} \times I_R$$

$$I_{\text{SC (peak asym)}} = K I_{\text{SC}} \quad \text{where}$$

$$K = \left\{ 1 + e^{-\left(\phi + \frac{\pi}{2}\right) \frac{r}{x} \sin \phi} \right\} \sqrt{2}, \text{ per unit}$$

$$\phi = \arctan \frac{x}{r}, \text{ radians}$$

Example of How to Calculate SC Current

Assume we have a transformer with a 69kV primary and the following known data:

Transformer MVA = 30 MVA base

Rated amps on LV (@ 30 MVA) = 1000 amps

Tested load loss @ 30 MVA: 72.0 kw

Tested impedance @ 30 MVA: 8.0% (= 0.08 p.u.)

To find I_{sc} (RMS symmetrical) and I_{sc} (Peak Asym), we must perform 3 steps in the following order:

1. Determine I_{sc} (RMS symmetrical)
2. Determine offset (asymmetrical) “K” factor
3. Apply derived data from 1. and 2. to determine peak offset asymmetrical amps.

Next



Example of How to Calculate SC Current

STEP 1: Find I_{SC} (RMS symmetrical)

Note: Z_T and Z_s are in p.u.

$$I_{SC} = \frac{I_R}{Z_T + Z_S}$$

$$I_{SC} = \frac{1000}{0.08 + 0} = 12,500A$$

OR, using the other formula ...

$$I_{SC} = \frac{100}{8\% + 0\%} \times I_{\text{rated}}$$

$$I_{SC} = \frac{100}{8\% + 0\%} \times 1000A = 12,500A$$

Symmetrical Current without Z_s

Symmetrical Current with Z_s

$$I_{SC} = \frac{I_R}{Z_T + Z_S}$$

$$I_{SC} = \frac{1000}{0.08 + Z_s}$$

$$Z_s = \frac{MVA_T}{MVA_S} = \frac{30}{9800} = 0.31\%$$

$$I_{SC} = \frac{1000}{0.08 + 0.0031} = 12,034 A$$

Note: Z_s is derived from C57.12.00-2010 Table 15 if not specified from customer.

Difference (with vs without Z_s) is almost 500A or 4%

Next

Example of How to Calculate SC Current

Step 2: Determine the “K” factor:

To find “K” factor, we need to determine %R and X/R ratio...

$$K = \left\{ 1 + \left[e^{-\left(\phi + \frac{\pi}{2}\right)\frac{r}{x}} \right] \sin \phi \right\} \sqrt{2}$$

1. Find %R

$$\%R = 100 \times \frac{\text{Load Loss (kW)}}{KVA_T} = \frac{100 \times 72}{30,000} = 0.24\%$$

2. Find X/R

$$\frac{X}{R} = \frac{Z_T}{\%R} = \frac{8\%}{0.24\%} = 33.33$$

Plug these values into next equation

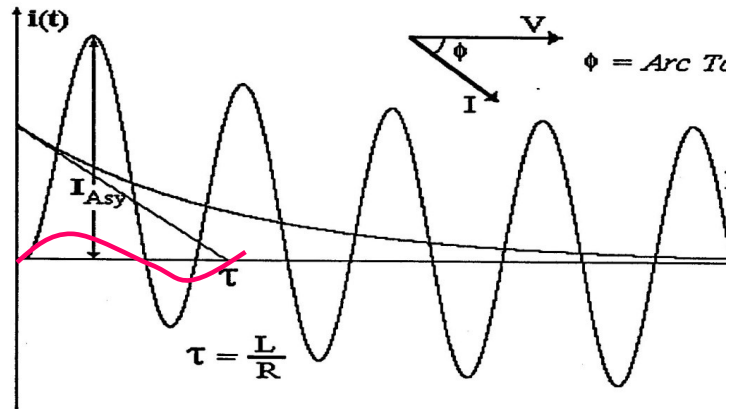
Example of How to Calculate SC Current

Step 2 (continued): Determine the “K” factor:

$$K = \left\{ 1 + \left[e^{-\left(\phi + \frac{\pi}{2}\right) \frac{r}{x}} \right] \sin \phi \right\} \sqrt{2}$$

$$K = \left\{ 1 + \left[e^{-\left(\tan^{-1}(33.33) + \frac{\pi}{2}\right) * \frac{1}{33.33}} \right] * \sin(\tan^{-1}(33.33)) \right\} * \sqrt{2}$$

$$K = 2.702$$



C57.12.00-2010 Table 14

x/r	K
1000.00	2.824
500.00	2.820
333.00	2.815
250.00	2.811
200.00	2.806
167.00	2.802
143.00	2.798
125.00	2.793
111.00	2.789
100.00	2.785
50.00	2.743
33.30	2.702

Example of How to Calculate SC Current

Step 3: Determine the I_{sc} (Peak Asymmetrical):

Since $I_{sc}(\text{peak asym}) = K \times I_{sc}(\text{RMS symmetrical})$

then ...

$$I_{sc}(\text{peak asym}) = 2.702 \times 12,500 \text{ amps} = \underline{33,750 \text{ amps}}$$

FYI: Since $F \propto I^2$

The Txf forces will see $(33750 \text{ amps} / (1000 \times \sqrt{2}) \text{ amps})^2 = (23.86)^2 = 569 \times \text{normal forces}$



Questions



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